Name:



# **Student Workbook**

Fall, 2022 - Pyret Edition



Workbook v3.0

Brought to you by the Bootstrap team:

- Emmanuel Schanzer
- Kathi Fisler
- Shriram Krishnamurthi
- Dorai Sitaram
- Joe Politz
- Ben Lerner
- Nancy Pfenning
- Flannery Denny
- Rachel Tabak

Visual Designer: Colleen Murphy

# Computing Needs All Voices!

The pioneers pictured below are featured in our Computing Needs All Voices lesson. To learn more about them and their contributions, visit https://bit.ly/bootstrap-pioneers.



We are in the process of expanding our collection of pioneers. If there's someone else whose work inspires you, please let us know at <a href="https://bit.ly/pioneer-suggestion">https://bit.ly/pioneer-suggestion</a>.

# Notice and Wonder

Write down what you notice and wonder from the What Most Schools Don't Teach video.

 $"Notices" should be statements, not questions. What stood out to you? What do you remember? \\ "Wonders" are questions.$ 

What do you Notice?	What do you Wonder?

# Windows and Mirrors

own identity and experience of the world. Write about who or what you connected with and why.
dentify something(s) from the film or the posters that served as a window for you, giving you insight into other people's experiences or
xpanding your thinking in some way.

# Reflection: Problem Solving Advantages of Diverse Teams

This reflection is designed to follow reading <u>LA Times Perspective</u> : A solution to tech's lingering diversity problem? Try thinking about ketchup  1) The author argues that tech companies with diverse teams have an advantage. Why?
2) What suggestions did the article offer for tech companies looking to diversify their teams?
3) What is one thing of interest to you in the author's bio?
4) Think of a time when you had an idea that felt out of the box. Did you share your idea? Why or why not?
5) Can you think of a time when someone else had a strategy or idea that you would never have thought of, but was interesting to you and/or pushed your thinking to a new level?
6) Based on your experience of exceptions to mainstream assumptions, propose another pair of questions that could be used in place of "Where do you keep your ketchup?" and "What would you reach for instead?".

# The Math Inside video games

- Video games are all about *change!* How fast is this character moving? How does the score change if the player collects a coin? Where on the screen should we draw a castle?
- We can break down a game into parts, and figure out which parts change and which ones stay the same. For example:
  - Computers use **coordinates** to position a character on the screen. These coordinates specify how far from the left (x-coordinate) and the bottom (y-coordinate) a character should be. Negative values can be used to "hide" a character, by positioning them somewhere off the screen.
  - When a character moves, those coordinates change by some amount. When the score goes up or down, it *also* changes by some amount.
- From the computer's point of view, the whole game is just a bunch of numbers that are changing according to some equations. We might not be able to see those equations, but we can definitely see the effect they have when a character jumps on a mushroom, flies on a dragon, or mines for rocks!
- Modern video games are *incredibly* complex, costing millions of dollars and several years to make, and relying on hundreds of programmers and digital artists to build them. But building even a simple game can give us a good idea of how the complex ones work!

# Notice and Wonder

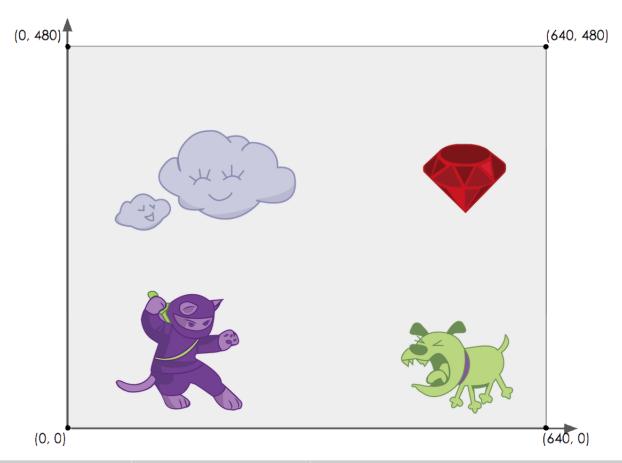
Write down what you notice and wonder about the Ninja Cat Game.

"Notices" should be statements, not questions. What stood out to you? What do you remember?

What do you Notice?	What do you Wonder?

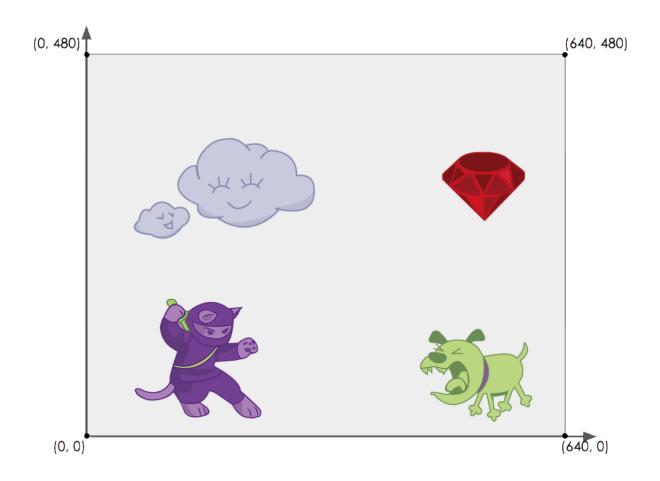
# Reverse Engineer a video game

What is changing in the game? What variables is the program keeping track of? The first example is filled in for you.



Thing in the Game	What Changes About It?	More Specifically what variable(s) are being tracked?	
Dog	Position	x-coordinate	

# **Estimating Coordinates**



The coordinates for the PLAYER (NinjaCat) are: (\_\_\_\_\_\_,\_\_\_\_\_)

# Brainstorm Your Own Game

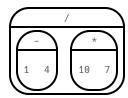
Created by:			
Background			
Our game takes place: In space? The desert? A mall?			
Player			
The Player is a			
The Player is a			
Target			
Your Player GAINS points when they hit The Target.			
The Target is a			
The Target moves only to the left or right.			
Danger			
Your Player LOSES points when they hit The Danger.			
The Danger is a			
The Danger moves only to the left or right.			
Artwork/Sketches/Proof of Concept			
Below is a 640x480 rectangle, representing your game screen.			
<ul> <li>Label the bottom-left corner as the coordinate (0,0).</li> <li>Label the other three corners with their corresponding coordinates.</li> </ul>			
<ul> <li>Label the other three corners with their corresponding coordinates.</li> <li>In the rectangle, sketch a picture of your game!</li> </ul>			

# Order of Operations

If you were to write instructions for getting ready for school, it would matter very much which instruction came first: putting on your socks, putting on your shoes, etc.

Sometimes we need multiple expressions in mathematics, and the order matters there, too! Mathematicians didn't always agree on the **Order of Operations**, but at some point it became important to develop rules to help them work together.

To help us organize our math into something we can trust, we can diagram a math expression using the **Circles of Evaluation**. For example, the expression  $(1-4) \div (10 \times 7)$  can be diagrammed as shown below.



Order of Operations is important when programming, too!

To convert a **Circle of Evaluation** into code, we walk through the circle from outside-in, moving left-to-right. We type an open parenthesis when we *start* a circle, and a close parenthesis when we *end* one. Once we're in a circle, we write whatever is on the left of the circle, then the **operation** at the top, and then whatever is on the right. The circle above, for example, would be programmed as ((1 - 4) / (10 \* 7)).

# Completing Circles of Evaluation from Arithmetic Expressions

For each expression on the left, finish the Circle of Evaluation on the right by filling in the blanks.

roi eaci	Arithmetic Expression	Circle of Evaluation on the right by filling in the blanks.  Circle of Evaluation
1	$4+2-\frac{10}{5}$	
2	$7-1+5 \times 8$	+ 7 1 *
3	$\frac{-15}{5+-8}$	/ + 5
4	$(4+(9-8)) \times 5$	* 4 9 8
5	$6 \times 4 + \frac{96}{5}$	4 9
*	$\frac{20}{6+4} - \frac{5 \times 9}{-12-3}$	20 + 3

# Matching Circles of Evaluation and Arithmetic Expressions

Draw a line from each Circle of Evaluation on the left to the corresponding arithmetic expression on the right.

**Circle of Evaluation** 

**Arithmetic Expression** 



1

Α

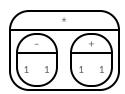
 $1 \div (1 \times 1)$ 



2

В

(1+1)-1



3

С

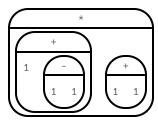
 $(1 \times 1) \div 1$ 



4

D

 $(1+(1-1)) \times (1+1)$ 



5

 $E (1-1) \times (1+1)$ 

# Translate Arithmetic to Circles of Evaluation & Code (Intro)

 $Translate\ each\ of\ the\ arithmetic\ expressions\ below\ into\ Circles\ of\ Evaluation, then\ translate\ them\ to\ Code.$ 

	Arithmetic	Circle of Evaluation	Code
1	$(3 \times 7) - (1+2)$		
2	3 – (1 + 2)		
3	3-(1+(5 × 6))		
4	$(1+(5 \times 6))-3$		

# Completing Partial Code from Circles of Evaluation

For each Circle of Evaluation on the left, finish the Code on the right by filling in the blanks.

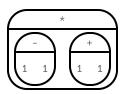
Tor cacir	Circle of Evaluation	the Code on the right by filling in the blanks.  Code
1	+ 16	(+ (6 *))
2	- + 25 13 2 4	(( + 13) ( 4))
3	* 28 10 4	(( + 4))
4	13 / / / / / / / / / / / / / / / / / / /	(13 (7 (24)))
5	+ / + 3 5 3	(((81)3)(53))
6	/ + 7 9 x 2 4	((+) / (*))

# Matching Circles of Evaluation & Code

Draw a line from each Circle of Evaluation on the left to the corresponding Code on the right.

**Circle of Evaluation** 

Code



1

Α

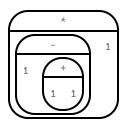
((1 - (1 + 1)) \* 1)



2

В

((1 - 1) \* (1 + 1))



3

С

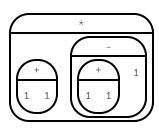
((1 + 1) \* ((1 + 1) - 1))



4

D

((1 + 1) - 1)



5

Ε

((1 - 1) + 1)

# Translate Arithmetic to Circles of Evaluation & Code 2

 $Translate\ each\ of\ the\ arithmetic\ expressions\ below\ into\ Circles\ of\ Evaluation, then\ translate\ them\ to\ Code.$ 

	Arithmetic	Circle of Evaluation	Code
1	6 × 8+(7-23)		
2	$18 \div 2 + 24 \times 4 - 2$		
3	$(22-7) \div (3+2)$		
4	$(24 \div 4) \times 2 - 6 + 20 \times 2$		

ω	N	ь		Trai	
$(50 \div 5) \times 2 - ((3+4) \times 2 - 5)$	$45-9 \times (3+(2-4))-7$	$\frac{16+3^2}{\sqrt{49-2}}$	Arithmetic	nslate each of the arithmetic expressions below ir	Arithmetic Ex
			Circle of Evaluation		Arithmetic Expressions to Circles of Evaluation & o
			Code	nctions are num-sqr and num-sqrt.	n & Code - Challenge

### **Introduction to Programming**

The **Editor** is a software program we use to write Code. Our Editor allows us to experiment with Code on the right-hand side, in the **Interactions Area**. For Code that we want to *keep*, we can put it on the left-hand side in the **Definitions Area**. Clicking the "Run" button causes the computer to re-read everything in the Definitions Area and erase anything that was typed into the Interactions Area.

#### **Data Types**

Programming languages involve different data types, such as Numbers, Strings, Booleans, and even Images.

- Numbers are values like 1, 0.4, 1/3, and -8261.003.
  - Numbers are usually used for quantitative data and other values are usually used as categorical data.
  - In Pyret, any decimal must start with a 0. For example, 0.22 is valid, but .22 is not.
- Strings are values like "Emma", "Rosanna", "Jen and Ed", or even "08/28/1980".
  - All strings must be surrounded in quotation marks.
- Booleans are either true or false.

All values evaluate to themselves. The program 42 will evaluate to 42, the String "Hello" will evaluate to "Hello", and the Boolean false will evaluate to false.

#### **Operators**

Operators (like +, -, \*, <, etc.) work the same way in Pyret that they do in math.

- Operators are written between values, for example: 4 + 2.
- In Pyret, operators must always have a space around them. 4 + 2 is valid, but 4+2 is not.
- If an expression has different operators, parentheses must be used to show order of operations. 4 + 2 + 6 and 4 + (2 \* 6) are valid, but 4 + 2 \* 6 is not.

#### **Applying Functions**

Applying functions works much the way it does in math. Every function has a name, takes some inputs, and produces some output. The function name is written first, followed by a list of arguments in parentheses.

- In math this could look like f(5) or g(10,4).
- In Pyret, these examples would be written as f(5) and g(10, 4).
- Applying a function to make images would look like star(50, "solid", "red").
- There are many other functions, for example num-sqr, num-sqrt, triangle, square, string-repeat, etc.

Functions have contracts, which help explain how a function should be used. Every contract has three parts:

- The Name of the function literally, what it's called.
- The Domain of the function what types of values the function consumes, and in what order.
- The Range of the function what type of value the function produces.

# **Numbers and Strings**

 $\label{eq:makesure you've loaded the $\underline{$\operatorname{code.pyret.org}(\operatorname{CPO})$, clicked "Run", and are working in the Interactions Area.}$ 

Numbers
1) Try typing 42 into the Interactions Area and hitting "Enter". What is the largest number the editor can handle?
2) Try typing 0.5. Then try typing .5. Then try clicking on the answer. Experiment with other decimals. Explain what you understand about
how decimals work in this programming language.
3) What happens if you try a fraction like 1/3 ?
4) Try writing <b>negative</b> integers, fractions and decimals. What do you learn?
Strings
String values are always in quotes.
5) Is 42 the same as "42" ? Why or why not? Write your answer below:
Try typing your name (in quotes!).
Try typing a sentence like "I'm excited to learn to code!" (in quotes!).  The trying a sentence with the appairing quote but without the plaine parts. Bead the agreement and the property of the plaine parts.
<ul> <li>Try typing your name with the opening quote, but without the closing quote. Read the error message!</li> <li>Now try typing your name without any quotes. Read the error message!</li> </ul>
6) Explain what you understand about how strings work in this programming language.
Operators
7) Just like math, Pyret has operators like $+$ , $-$ , $*$ and $/$ . Try typing in $4+2$ , and then $4+2$ (without the spaces). What can you conclude from this?
8) Type in the following expressions, one at a time: 4 + 2 * 6 , (4 + 2) * 6 , 4 + (2 * 6) . What do you notice?
9) Try typing in 4 + "cat", and then "dog" + "cat". What can you conclude from this?

# **Booleans**

Boolean-producing expressions are yes-or-no questions and will always evaluate to either true ("yes") or false ("no"). What will each of the expressions below evaluate to? Write down your prediction in the blanks provided and then type the code into the Interactions Area to see what it returns.

	Prediction	Result		Prediction	Result
1) 3 <= 4			2) "a" > "b"		
3) 3 == 2			4) "a" < "b"		
5) 2 < 4			6) "a" == "b"		
7) 5 >= 5			8) "a" <> "a"		
9) 4 >= 6			10) "a" >= "a"		
11) 3 <> 3			12) "a" <> "b"		
13) In your own words, describe what < does.					
14) In your own words, describe what >= does.					
15) In your own words, describe what <> does.					
			Predicti	on:	Result:
16) string-contains("catnap", "cat")					
17) string-contains("cat", "catnap")					
18) How many <b>Numbers</b> are there in the entire universe?					
19) How many <b>Strings</b> are there in the entire universe?					
20) How many <b>Booleans</b> are there in the entire universe?					

# Applying Functions

Type this line of code into the Interactions Area and hit "Enter":
triangle(50, "solid", "red")
1) What is the name of this function?
2) What did the expression evaluate to?
3) How many arguments does triangle expect?
4) What data type does the triangle function produce?
Catching Bugs
The following lines of code are all BUGGY! Read the code and the error messages to identify the mistake. 5) triangle(20, "solid" "red")
Pyret didn't understand your program around triangle(20, "solid" "red")
Can you spot the mistake?
6) triangle(20, "solid")  This application expression errored:  triangle(20, "solid")  2 arguments were passed to the operator. The operator evaluated to a function accepting 3 parameters. An application expression expects the number of parameters and arguments to be the same.
Can you spot the mistake?
7) triangle(20, 10, "solid", "red")  This application expression errored:  triangle(20, 10, "solid", "red")`  A arguments were passed to the operator. The operator evaluated to a function accepting 3 parameters. An application expression expects the number of parameters and arguments to be the same.
Can you spot the mistake?
8) triangle (20, "solid", "red")  Pyret thinks this code is probably a function call:  triangle (20, "solid", "red")  Function calls must not have space between the function expression and the arguments.
Can you spot the mistake?

# Frayer Model: Domain and Range My Definition Facts and Characteristics Domain Examples Non-Examples My Definition **Facts and Characteristics** Range Examples Non-Examples

# Practicing Contracts: Domain & Range

Consider the following contract:
is-beach-weather :: Number, String -> Boolean
1) What is the <b>Name</b> of this function?
2) How many arguments are in this function's <b>Domain</b> ?
3) What is the <b>Type</b> of this function's <b>first argument</b> ?
4) What is the <b>Type</b> of this function's <b>second argument</b> ?
5) What is the <b>Range</b> of this function?
6) Circle the expression below that shows the correct application of this function, based on its contract.
<pre>A. is-beach-weather(70, 90) B. is-beach-weather(80, 100, "cloudy") C. is-beach-weather("sunny", 90) D. is-beach-weather(90, "stormy weather")</pre>
Consider the following contract:
cylinder :: Number, Number, String -> Image
7) What is the <b>Name</b> of this function?
8) How many arguments are in this function's <b>Domain</b> ?
9) What is the <b>Type</b> of this function's <b>first argument</b> ?
10) What is the <b>Type</b> of this function's <b>second argument</b> ?
11) What is the <b>Type</b> of this function's <b>third argument</b> ?
12) What is the <b>Range</b> of this function?
13) Circle the expression below that shows the correct application of this function, based on its contract.
<pre>A. cylinder("red", 10, 60) B. cylinder(30, "green") C. cylinder(10, 25, "blue") D. cylinder(14, "orange", 25)</pre>

# Matching Expressions and Contracts

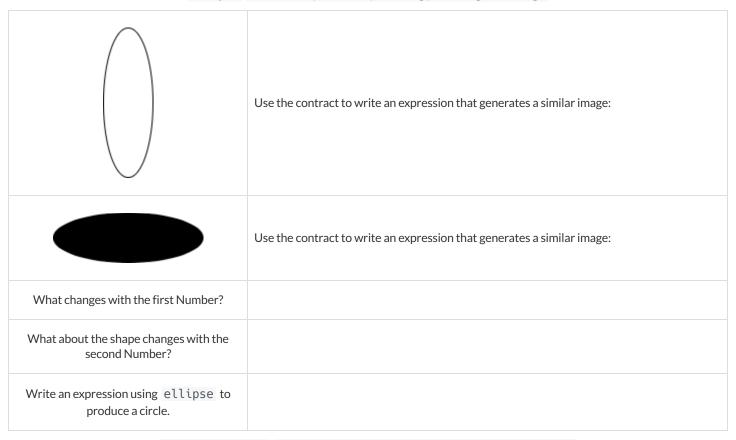
*Match* the contract (left) with the expression described by the function being used (right).

Contract		Expression
<pre># make-id :: String, Number -&gt; Image</pre>	1 A	make-id("Savannah", "Lopez", <b>32</b> )
<pre># make-id :: String, Number, String -&gt; Image</pre>	2 B	make-id("Pilar", <b>17</b> )
<pre># make-id :: String -&gt; Image</pre>	3 C	make-id("Akemi", 39, "red")
<pre># make-id :: String, String -&gt; Image</pre>	4 D	make-id("Raïssa", "McCracken")
<pre># make-id :: String, String, Number -&gt; Image</pre>	5 E	make-id("von Einsiedel")

Contract	Expression
<pre># is-capital :: String, String -&gt; Boolean</pre>	6 A show-pop("Juneau", "AK", 31848)
<pre># is-capital :: String, String, String -&gt; Boolean</pre>	7 B show-pop("San Juan", 395426)
<pre># show-pop :: String, Number -&gt; Image</pre>	8 C is-capital("Accra", "Ghana")
<pre># show-pop :: String, String, Number -&gt; Image</pre>	9 D show-pop(3751351, "Oklahoma")
<pre># show-pop :: Number, String -&gt; Number</pre>	10 E is-capital("Albany", "NY", "USA")

# **Using Contracts**

ellipse :: Number, Number, String, String -> Image



regular-polygon :: Number, Number, String, String -> Image

	Use the contract to write an expression that generates a similar image:
	Use the contract to write an expression that generates a similar image:
What changes with the first Number?	
What about the shape changes with the second Number?	
Use regular-polygon to write an expression for a square!	
How would you describe a <b>regular polygon</b> to a friend?	

# Triangle Contracts

1) What kind of triangle does the	e triangle function produce?
There are lots of other kinds of t	riangles! And Pyret has lots of other functions that make triangles!
triangle :: (size:: Num	mber, style :: String, color :: String) -> Image
right-triangle :: (base	e::Number, height::Number, style::String, color::String) -> Image
isosceles-triangle ::	<pre>(leg::Number, angle::Number, style::String, color::String) -&gt; Image</pre>
2) Why do you think triangle triangle-sas needs three?	e only needs one number, while right-triangle and isosceles-triangle need two numbers and
2) Write right triangle of	various for the images below. One argument for each should be 100
3) Write right-triangle ex	xpressions for the images below. One argument for each should be 100 .
	ersin right-triangle represent?
5) Write isosceles-triang	le expressions for the images below. 1 argument for each should be $100$ .
6) What do you think the numbe	ersin isosceles-triangle represent?
7) Write 2 expressions that would for the other expression.	Id build <b>right-isosceles</b> triangles. Use right-triangle for one expression and isosceles-triangle

# Radial Star

```
radial-star :: (
    points :: Number,
    inner-radius :: Number,
    full-radius :: Number,
    style :: String,
    color :: String
) -> Image
```

Using the detailed contract above, match each image to the expression that describes it.

Image			Expression
*	1	А	radial-star(5, 50, 200, "solid", "black")
*	2	В	radial-star(7, 100, 200, "solid", "black")
	3	С	radial-star(7, 100, 200, "outline", "black")
	4	D	radial-star(10, 150, 200, "solid", "black")
	5	E	radial-star(10, 20, 200, "solid", "black")
*	6	F	radial-star(100, 20, 200, "outline", "black")
	7	G	radial-star(100, 100, 200, "outline", "black")

What's on your mind?

# **Diagramming Function Composition**

<pre>f :: Number -&gt; Number Consumes a number, multiplies by 3 to produce the result</pre>	<pre>g :: Number -&gt; Number Consumes a number, adds six to produce the result</pre>	h :: Number -> Number Consumes a number, subtracts one to produce the result
f(x) = 3x	g(x) = x + 6	h(x) = x - 1

For each function composition diagrammed below, translate it into the equivalent Circle of Evaluation for Order of Operations. Then write expressions for *both* versions of the Circles of Evaluation, and evaluate them for x = 4. The first one has been completed for you.

Function Composition	rsions of the Circles of Evaluation, and evaluate Order of Operations		anslate & Evaluate
1)	-	Composition:	h(g(f(x)))
g f x	$ \begin{array}{ c c } \hline f \\ \hline x \\ \hline   & 6 \end{array} $	Operations:	((3 * x) + 6) - 1
		Evaluate for x = 4	h(g(f(4))) = 17
2) g		Composition:	
h x		Operations:	
		Evaluate for x = 4	
3)		Composition:	
	Operations:		
		Evaluate for x = 4	
4)		Composition:	
h g x		Operations:	
		Evaluate for x = 4	

# Function Composition — Green Star

1) Draw a Circle of Evaluation and write the Code for a **solid**, **green star**, **size 50**. **Circle of Evaluation**:

Code:	
Using the star described above as the <b>original</b> , draw the Circles of Eval	uation and write the Code for each exercise below.
2) A solid, green star, that is triple the size of the original (using scale )	3) A solid, green star, that is half the size of the original (using scale )
4) A solid, green star of size 50 that has been rotated 45 degrees counter-clockwise	5) A solid, green star that is 3 times the size of the original and has been rotated 45 degrees

# Function Composition — Your Name

You'll be investigating these functions with your partner:

```
# text :: String, Number, String -> Image
# flip-horizontal :: Image -> Image
# flip-vertical :: Image -> Image
# beside :: Image, Image -> Image
# beside :: Image, Image
```

1) In the editor, write the code to make an image of your name in big letters in a color of your choosing using text. Then draw the Circle of Evaluation and write the Code that will create the image.

Circle of Evaluation for an "image of your name":

Using the "image of your name" described above as the <b>original</b> , draw the Circles of Evaluation and write the Code for each exercise below. Test your ideas in the editor to make sure they work.					
2) The framed "image of your name".	3) The "image of your name" flipped vertically.				
4) The "image of your name" above "the image of your name" flipped vertically.	5) The "image of your name" flipped horizontally beside "the image of your name".				

# $Function\,Composition-scale-xy$

You'll be investigating these two functions with your partner:

# scale-xy :: Number, Number, Image -> Image

# overlay :: Image, Image -> Image

The Image:	Circle of Evaluation:	Code:	
•	rhombus 40 90 "solid" "purple"	rhombus(40, 90, "solid", "purple")	

Starting with the image described above, write the Circles of Evaluation and Code for each exercise below. Be sure to test your code in the editor!

cultor.	
1) A purple rhombus that is stretched 4 times as wide.	2) A purple rhombus that is stretched 4 times as tall
3) The tall rhombus from #1 overlayed on the wide rhombus (#2).	★ Overlay a red rhombus onto the last image you made in #3.

# More than one way to Compose an Image!

What image will each of the four expressions below evaluate to? If you're not sure, type them into the Interactions Area and see if you can figure out how the code constructs its image.

```
scale(2, rectangle(100, 100, "solid", "black"))
                                                                                                                                                                                                                                                                                                             scale-xy(1, 2, square(100, "solid", "black"))
                                                                                                                                                                                                                                                                                                                                                                                         beside(rectangle(200, 100, "solid", "black"), square(100, "solid", "black"))
                                                                                                                  rectangle(100, 50, "solid", "black"),
                                                                                   above(
rectangle(200, 100, "solid", "black"),
rectangle(100, 50, "solid", "black")))
```

For each image below, identify 2 expressions that could be used to compose it. The bank of expressions at the top of the page includes one possible option for each image.

*	ω	N	ь

## **Defining Values**

In math, we use **values** like -98.1, 2/3 and 42. In math, we also use **expressions** like  $1 \times 3$ ,  $\sqrt{16}$ , and 5 - 2. These evaluate to results, and typing any of them in as code produces some answer.

Math also has **definitions**. These are different from values and expressions, because *they do not produce results*. Instead, they simply create names for values, so that those names can be re-used to make the Math simpler and more efficient.

Definitions always have both a name and an expression. The name goes on the left and the value-producing expression goes on the right, separated by an equals sign:

```
  \begin{aligned}
    x &= 4 \\
    y &= 9 + x
  \end{aligned}
```

The name is defined to be the result of evaluating the expression. Using the above examples, we get "x is defined to be 4, and y is defined to be 13. Important: there is no "answer" to a definition, and typing in a definition as code will produce no result.

Notice that definitions can refer to previous definitions. In the example above, the definition of y refers to x. But x, on the other hand, cannot refer to y. Once a value has been defined, it can be used in later expressions.

In Pyret, these definitions are written the exact same way:

Try typing these definitions into the Definitions Area on the left, clicking "Run", and then using them in the Interactions Area on the right.

```
x = 4
y = 9 + x
```

Just like in math, definitions in our programming language can only refer to previously-defined values.

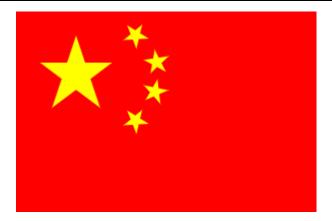
Here are a few more value definitions. Feel free to type them in, and make sure you understand them.

```
x = 5 + 1
y = x * 7
food = "Pizza!"
dot = circle(y, "solid", "red")
```

# Defining Values - Explore

Open the <u>Defining Values Starter File</u> and click "Run".  1) What do you Notice?
2) What do you Wonder?
Look at the expressions listed below. Think about what you expect each of them to produce. Then, test them out one at a time in the Interactions Area.
• X
• x + 5
• y - 9
• x * y
• Z
• t
• gold-star
• my-name
• swamp
• C
3) What have you learned about defining values?
4) Define at least 2 more variables in the Definitions Area, click "Run" and test them out. Once you know they're working, record the code yo used below.

### Defining Values - Chinese Flag



1) What image do you see repeated in the flag?

2) In the code below, highlight or circle all instances of the expression that makes the repeated image.

```
china =
  put-image(
    rotate(40,star(15,"solid","yellow")),
    120, 175,
    put-image(
      rotate(80,star(15,"solid","yellow")),
      140, 150,
      put-image(
        rotate(60, star(15, "solid", "yellow")),
        140, 120,
        put-image(
          rotate(40,star(15,"solid","yellow")),
          120, 90,
          put-image(scale(3,star(15,"solid","yellow")),
            60, 140,
            rectangle(300, 200, "solid", "red"))))))
```

3) Write the code to define a value for the repeated expression.

4) Open the Chinese Flag Starter File and click "Run".

- Type china into the Interactions Area and click Enter.
- Save a copy of the file, and simplify the flag code using the value you defined.
- Click "Run", and confirm that you still get the same image as the original.
- Now change the color of all of the stars to black, in both files.
- Then change the size of the stars.
- 5) Why is it helpful to define values for repeated images?

### Challenge:

- This file uses a function we haven't seen before! What is it?
- Can you figure out its contract? Hint: Focus on the last instance of the function.

# 1) Complete the table using the first row as an example.

2) Write the code to define the value of sunny.

Code: overlay(text("sun", 30, "black"), radial-star(30, 20, 50, "solid", "yellow"))	text radial-star "sun" 30 "black" 30 20 50 "solid" "yellow"	Code: frame(radial-star(30, 20, 50, "solid", "yellow"))	radial-star 30 20 50 "solid" "yellow"	Code: scale(3, radial-star(30, 20, 50, "solid", "yellow"))	scale  radial-star  30 20 50 "solid" "yellow"	Original Circle of Evaluation & Code
<b>1</b>	1	<b>↓</b>	$\downarrow$	<b>↓</b>	<b>↓</b>	<b>\</b>
Code:		Code:		<pre>Code: scale(3, sunny)</pre>	scale 3 sunny	Use the defined value sunny to simplify!

### Which Value(s) Would it Make Sense to Define?

For each of the images below, identify which element(s) you would want to define before writing code to compose the image. Hint: what gets repeated?



## Writing Code using Defined Values

1) On the line below, write the Code to define PRIZE-STAR as a pink, outline star of size 65.

Using the PRIZE-STAR definition from above, draw the Circle of Evaluation and write the Code for each of the exercises. One Circle of Evaluation has been done for you.

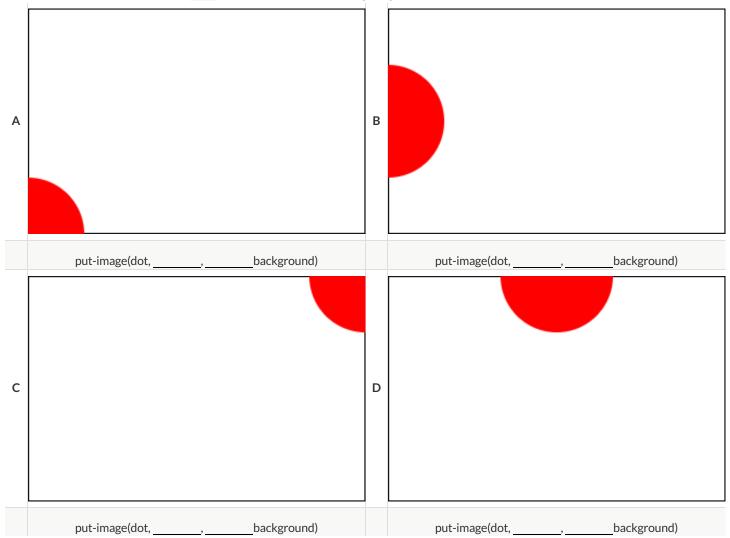
2 The outline of a pink star that is three times the size of the original (using scale)  Circle of Evaluation:  Scale  3 PRIZE-STAR	3 The outline of a pink star that is half the size of the original (using scale ) Circle of Evaluation:
Code:	Code:
4 The outline of a pink star that is rotated 45 degrees (It should be the same size as the original.)  Circle of Evaluation:	5 The outline of a pink star that is three times as big as the original and has been rotated 45 degrees Circle of Evaluation:
Code:	Code:
6) How does defining values help you as a programmer?	

### **Estimating Coordinates**

```
dot = circle(50, "solid", "red")
background = rectangle(300, 200, "outline", "black")
```

Think of the background image as a sheet of graph paper with the origin (0,0) in the bottom left corner. The width of the rectangle is 300 and the height is 200. The numbers in put-image specify a point on that graph paper, where the center of the top image (in this case dot) should be placed.

Estimate: What coordinates for the dot created each of the following images?



### **Decomposing Flags**

Each of the flags below is shown with their width and height. Identify the shapes that make up each flag. Use the flag's dimensions to estimate the dimensions of the different shapes. Then estimate the x and y coordinates for the point at which the center of each shape should be located on the flag. Hint: The bottom left corner of each flag is at (0,0) and the top right corner is given by the flags dimensions.

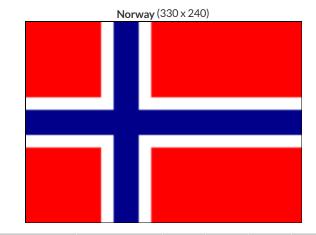


	Chile (420 x 280)
*	

shape:	color:	width:	height:	х	У

shape:	color:	width:	height:	х	У





shape:	color:	width:	height:	х	у

shape:	color:	width:	height:	x	у

## Notice and Wonder

As you investigate the <u>Blank Game Starter File</u> with your partner, record what you Notice, and then what you Wonder. Remember, "Notices" are statements, not questions.

What do you Notice?	What do you Wonder?

# The Great gt domain debate!

 $\textbf{Kermit:} \ The \ domain \ of \ gt \ is \ Number, \ String, \ String \ .$ 

Oscar: The domain of gt is Number.
Ernie: I'm not sure who's right!
In order to make a triangle, we need a size, a color and a fill style
but all we had to tell our actor was $gt(20)$ and they returned $triangle(20, "solid", "green")$ .
Please help us!
1) What is the correct domain for gt?
2) What could you tell Ernie to help him understand how you know?

## Let's Define Some New Functions!

1) Let's define a function rs to generate solid red squares of whatever size we give them!

If I say rs(5), what would our actor need to say?

Let's write a few more examples:	
rs() →	
rs() →	
$rs($ $) \rightarrow$	
What changes in these examples? Name your variable(s):	
Let's define our function using the variable.	
fun rs():	end
2) Let's define a function bigc to generate big solid circles of size 100 in whatever color we give them! If I say bigc("orange"), what would our actor need to say?	
Let's write a few more examples:	
bigc() →	
bigc() →	
bigc() →	
What changes in these examples? Name your variable(s):  Let's define our function using the variable.	
fun bigc():	end
3) Let's define a function ps to build a pink star of size 50, with the input determining whether it's solid or o	utline!
If I say ps("outline"), what would our actor need to say?	
Write examples for all other possible inputs:	
ps() →	
ps() →	
What changes in these examples? Name your variable(s):	
Let's define our function using the variable.	
fun ps():	end end
Add these new function definitions to your <u>gt Starter File</u> and test them out!	

### Let's Define Some More New Functions!

1) Let's define a function sun to write SUNSHINE in whatever color and size we give it!

If I say sun(5, "blue"), what would our actor need to say?

4) Add these new function definitions to your <u>gt Starter File</u> and test them out!

Let's write a few more examples: sun( ,  $) \rightarrow$ What changes in these examples? Name your variable(s): Let's define our function using the variable. fun sun( , ): 2) Let's define a function me to generate your name in whatever size and color we give it! If I say me(18, "gold"), what would our actor need to say? Let's write a few more examples: me( ,  $) \rightarrow$ me( ,  $) \rightarrow$  $\mathsf{me}( \hspace{1cm} , \hspace{1cm} ) \rightarrow$ What changes in these examples? Name your variable(s): Let's define our function using the variable. fun me( , ): 3) Let's define a function gr to build a solid, green rectangle of whatever length and width we give it! If I say gr(10, 80), what would our actor need to say? Let's write a few more examples:  $gr( , ) \rightarrow rectangle( , , "solid", "green")$  $gr( , ) \rightarrow rectangle( , , "solid", "green")$  $gr( , ) \rightarrow rectangle( , , "solid", "green")$ What changes in these examples? Name your variable(s): Let's define our function using the variable. fun gr(\_\_\_\_\_, \_\_\_\_): \_\_\_\_\_\_\_end

# Describe and Define Your Own Functions!

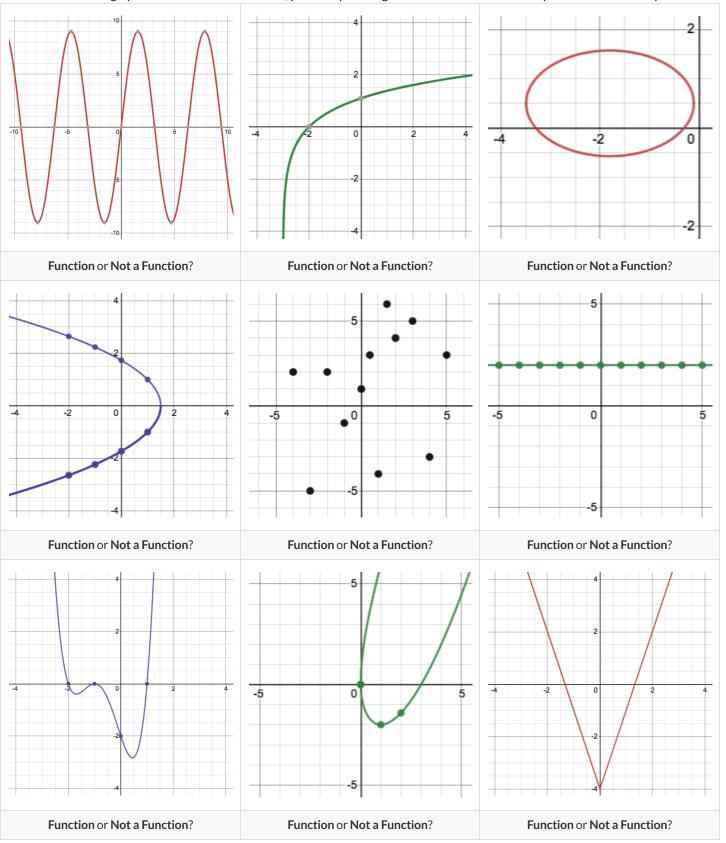
1) Let's define a function	to generate	
If I say, what would Let's write a few more examples:	d our actor need to say?	
·	,	
	(	)
	(	)
<u> </u>	(	)
What variable changes?		
Let's define our function using the variable		
fun () :	(	_) end
2) Let's define a function	to generate	
If I say, what would Let's write a few more examples:	d our actor need to say?	
( <u></u> )→	(	)
(	(	)
	(	
What variable changes?		
fun () :	(	) end
3) Let's define a function	to generate	
If I say, what would	d our actor need to say?	
Let's write a few more examples:		
() ->	(	)
<u> </u>	(	)
(	(	)
What variable changes?		
Let's define our function using the variable		
fun ( ):	(	) end
Add your new function definitions to your gt \$	Starter File and test them out!	

46

What's on your mind?			

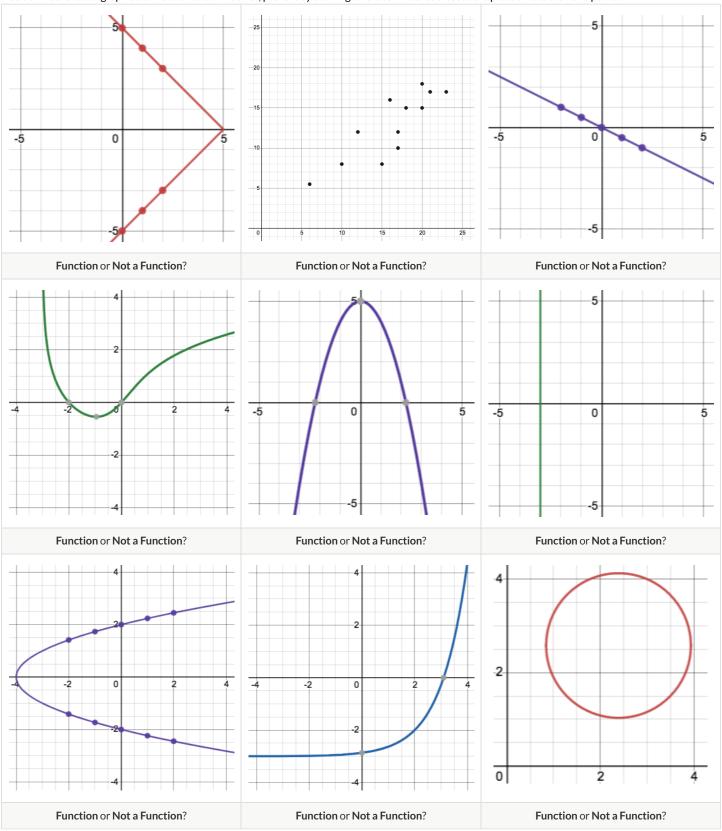
# Identifying Functions from Graphs

Decide whether each graph below is a function. If it's not, prove it by drawing a vertical line that crosses the plot at more than one point.



### Identifying Functions from Graphs (continued)

Decide whether each graph below is a function. If it's not, prove it by drawing a vertical line that crosses the plot at more than one point.



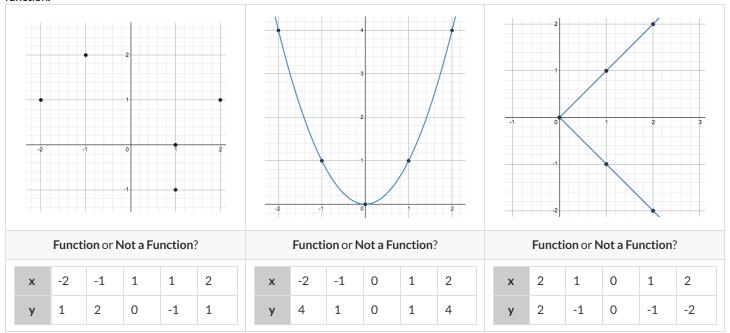
### Notice and Wonder - Functions

Write down what you Notice and Wonder about the graphs you've just seen. At a later point you will *also* use this page to record what you notice and wonder about the tables you'll see. *Remember: "Notices" should be statements, not questions!* 

What do you Notice?	What do you Wonder?

### How Tables Fail the Vertical Line Test

1) Each of the graphs below is also represented by a table. Use the vertical line test to determine whether or not each graph represents a function.



- 2) For each graph that failed the vertical line test, label the offending points with their coordinates.
- 3) Find the same coordinates in the table below the graph and circle or highlight them.
- 4) What do the tables of the non-functions have in common? What could you look for in other tables to identify whether or not they could represent a function?

5) Use the process you just described to determine whether each table below could represent a function. Circle or highlight the points that would end up on the same vertical line.

x	У
0	-2
1	-2
2	-2
3	-2
4	-2

le	€.	
	x	У
	0	-2
	1	1
	2	4
	3	7
	3	10

x	У
0	3
1	4
-1	5
2	6
-2	7

x	У	
1	0	
0	1	
1	2	
2	3	
3	4	

Function or Not?

Function or Not?

Function or Not?

Function or Not?

## Identifying Functions from Tables

Decide whether or not each table below could represent a function. If not, circle what you see that tells you it's not a function. In a function, there is exactly one y-value (or output) for each x-value (or input). If a table has more than one y-value (or output) for the same x-value (or input), it can not represent a function.

x	У
0	3
1	2
2	5
3	6
4	5

x	У
5	3
1	4
-3	5
3	6
2	7

input	output
0	2
5	2
2	2
6	2
3	2

x	У
1	0
1	1
1	2
1	3
1	4

Funct	ion	or	No	t?

Function or Not?

Function or Not?

tickets	\$
2	0
1	2
2	4
3	6
4	8

input	output
-4	-2
-3	-1
-2	0
-1	1
0	2

x	У
10	9
3	2
9	8
17	16
3	5

С	F
-40	-40
0	32
10	50
37	98.6
100	212

Function or Not?

### Function or Not?

### Function or Not?

### Function or Not?

input	output
0	7
-1	2
4	3
8	6
-5	-8

\$	games
10	5
11	25
12	45
13	65
14	85

x	y
8	10
6	5
4	0
6	-5
8	-10

miles	minutes
0	0
1	2
2	4
3	6
4	8

Function or Not?

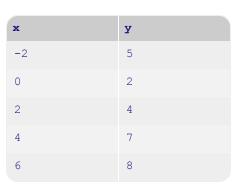
Function or Not?

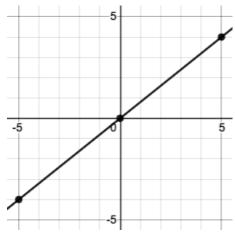
Function or Not?

Function or Not?

### Identifying Functions from Tables & Graphs

Decide whether or not each table or graph below could represent a function. If not, circle what tells you it's not a function. In a function, there is exactly one y-value for each x-value. If a table has more than one y-value for the same x-value, it can not represent a function.



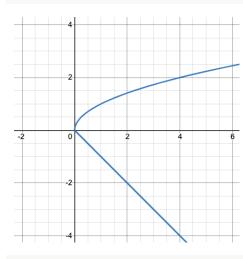


x	У
0	7
1	2
1	3
2	6
3	-8

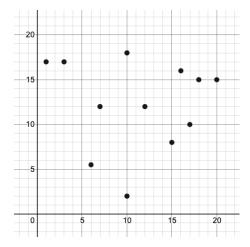
### Function or Not?

Function or Not?

Function or Not?



x	У
-1.5	-2
-1	-1
-0.5	0
0	1
0.5	2

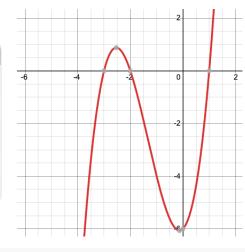


Function or Not?

Function or Not?

### Function or Not?

×	У
	1
-1	1.5
0	1.5
1	1.5
2	1.5
3	1.5



ж	У
8	1
5	2
4	3
5	4
8	5

Function or Not?

Function or Not?

Function or Not?

# Matching Examples and Definitions (Math)

Match each of the function definitions on the left with the corresponding table on the right. It may help to circle or highlight what's changing in the f(x) column of the table!

Function Definitions Example Tables

f(x) = x - 2

1

Δ

 x
 f(x) 

 1
  $2 \times 1$  

 2
  $2 \times 2$  

 3
  $2 \times 3$ 

f(x) = 2x

2

В

 x
 f(x) 

 15
 15-2 

 25
 25-2 

 35
 35-2

f(x) = 2x + 1

3

С

x	f(x)
10	2 + 10
15	2 + 15
20	2 + 20

f(x) = 1 - 2x

4

D

x	f(x)
0	1 - 2(0)
1	1 – 2(1)
2	1 – 2(2)

f(x) = 2 + x

5

Ε

$$x$$
  $f(x)$   
10  $2(10) + 1$   
20  $2(20) + 1$   
30  $2(30) + 1$ 

# Function Notation - Substitution

Complete the table below, by substituting the given value into the expression and evaluating.

Function Definition	Expression	Substitution	Evaluates to
f(x) = x + 2	<i>f</i> (3)	3+2	5
g(x) = x - 1	g(6)		
h(x) = 3x	h(4)		
k(x) = 2x - 1	k(5)		

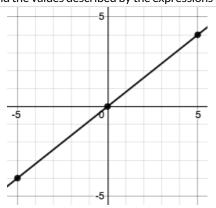
Now that you understand how to evaluate an expression, let's get some more practice! The table below includes four different functions. Beneath each of them are a collection of different expressions to evaluate.

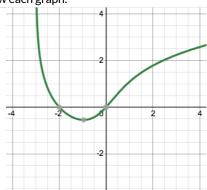
m(x) = -2x + 3	n(x) = -x + 7	v(x) = 10x - 8	$w(x) = x^2$
m(3) = -2(3) + 3	n(5) =	v(7) =	<i>w</i> (−2) =
-3			
m(-4) =	n(-2) =	v(0) =	w(10) =
m(0) =	n(3.5) =	v(-10) =	w(0) =
m(0.5) =	n(0) =	v(2.5) =	w(1.5) =

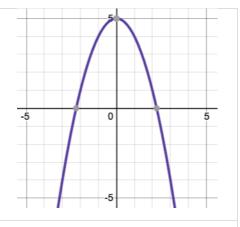
What do you Notice?	What do you Wonder?	

### Function Notation - Graphs

Find the values described by the expressions below each graph.



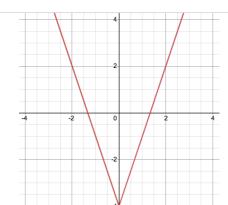


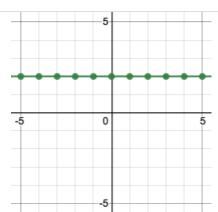


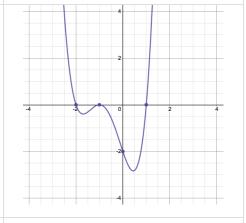
$$g(-2) =$$
\_\_\_\_\_

$$h(0) =$$
\_\_\_\_\_

$$h(1) =$$
\_\_\_\_\_

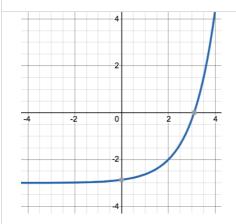


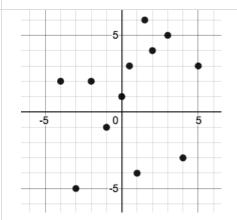


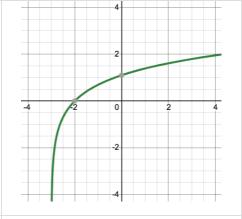


$$m(0) =$$
\_\_\_\_\_

$$m(1) =$$
\_\_\_\_\_







$$w(-2) =$$
\_\_\_\_\_

$$n(-\infty) = \underline{\hspace{1cm}}$$

$$w(0) =$$
\_\_\_\_\_

### **Function Notation - Tables**

Find the values described by the expressions below each table. Note: not all of the relationships here are actually functions!

x	f(x)
0	0
1	2
2	4
3	6
4	8

x	g(x)
5	3
1	4
-3	5
3	6
2	7

x	h(x)
0	2
5	2
2	2
6	2
3	2

$$g(1) = _{\underline{\hspace{1cm}}}$$

$$h(0) =$$
\_\_\_\_\_

$$y(1) = \frac{0?1?2?}{3?}$$

$$g(3) =$$
\_\_\_\_\_

$$h(3) =$$
\_\_\_\_\_

а	b(a)
-4	-2
-3	-1
-2	0
-1	1
0	2

С	d(c)
0	3
1	2
2	5
3	6
4	5

$$d(2) =$$
\_\_\_\_\_

$$m(0) =$$
\_\_\_\_\_

$$p(1) = _{\underline{\hspace{1cm}}}$$

$$d(4) =$$

$$m(-3) =$$
\_\_\_\_\_

S	r(s)
0	7
-1	2
4	3
8	6
-5	-8

$$r(-1) =$$

$$z(6) =$$
\_\_\_\_\_

$$l(10) =$$
\_\_\_\_\_

$$r(8) =$$
\_\_\_\_\_

$$v(14) =$$
\_\_\_\_\_

$$z(2) =$$
\_\_\_\_\_

$$l(3) =$$
\_\_\_\_\_

### **Defining Functions**

Functions can be viewed in *multiple representations*. You already know one of them: Contracts, which specify the Name, Domain, and Range of a function. Contracts are a way of thinking of functions as a *mapping* between one set of data and another. For example, a mapping from Numbers to Strings:

```
f :: Number -> String
```

Another way to view functions is with Examples. Examples are essentially input-output tables, showing what the function would do for a specific input:

In our programming language, we focus on the last two columns and write them as code:

```
examples:
    f(1) is 1 + 2
    f(2) is 2 + 2
    f(3) is 3 + 2
    f(4) is 4 + 2
end
```

Finally, we write a formal **function definition** ourselves. The pattern in the Examples becomes *abstract* (or "general"), replacing the inputs with variables. In the example below, the same definition is written in both math and code:

```
f(x) = x + 2
fun f(x): x + 2 end
```

Look for connections between these three representations!

- The function name is always the same, whether looking at the Contract, Examples, or Definition.
- The number of inputs in the Examples is always the same as the number of types in the Domain, which is always the same as the number of variables in the Definition.
- The "what the function does" pattern in the Examples is almost the same in the Definition, but with specific inputs replaced by variables.

# Matching Examples and Contracts

Match each set of examples (left) with the contract that best describes it (right).

Examples Contract

# end examples: f(24) **is** 24 / 2 f(5) **is** 5 / 2 f(9) **is** 9 / 2

N

ω

O

ш

5

### Matching Examples and Function Definitions

Highlight the variables in  $\ensuremath{\,^{\mid}} gt$  and label them with the word "size".

### examples:

```
gt(20) is triangle(20, "solid", "green")
gt(50) is triangle(50, "solid", "green")
```

end

```
fun gt(size): triangle(size, "solid", "green") end
```

Highlight and label the variables in the example lists below. Then, using gt as a model, match the examples to their corresponding function definitions.

definitions.			
Examples			Definition
<pre>examples:    f("solid") is circle(8, "solid", "red")    f("outline") is circle(8, "outline", "red") end</pre>	1	Α	<pre>fun f(s): star(s, "outline", "red") end</pre>
examples:     f(2) is 2 + 2     f(4) is 4 + 4     f(5) is 5 + 5 end	2	В	<pre>fun f(num): num + num end</pre>
<pre>examples:   f("red") is circle(7, "solid", "red")   f("teal") is circle(7, "solid", "teal") end</pre>	3	С	<pre>fun f(c): star(9, "solid", c) end</pre>
<pre>examples:    f("red") is star(9, "solid", "red")    f("grey") is star(9, "solid", "grey")    f("pink") is star(9, "solid", "pink") end</pre>	4	D	<pre>fun f(s): circle(8, s, "red") end</pre>
<pre>examples:   f(3) is star(3, "outline", "red")   f(8) is star(8, "outline", "red") end</pre>	5	E	<pre>fun f(c): circle(7, "solid", c) end</pre>

### **Creating Contracts From Examples**

Write the contracts used to create each of the following collections of examples.

```
examples:
  big-triangle(100, "red") is triangle(100, "solid", "red")
  big-triangle(200, "orange") is triangle(200, "solid", "orange")
2) __
examples:
  purple-square(15) is rectangle(15, 15, "outline", "purple")
  purple-square(6) is rectangle(6, 6, "outline", "purple")
end
3)
examples:
  banner("Game Today!") is text("Game Today!", 50, "red")
  banner("Go Team!") is text("Go Team!", 50, "red")
  banner("Exit") is text("Exit", 50, "red")
end
4)
examples:
  twinkle("outline", "red") is star(5, "outline", "red")
twinkle("solid", "pink") is star(5, "solid", "pink")
  twinkle("outline", "grey") is star(5, "outline", "grey")
examples:
  half(5) is 5 / 2
  half(8) is 8 / 2
  half(900) is 900 / 2
end
```

# Contracts, Examples & Definitions - bc

r	-	ľ	۲
в	_		ı

**Directions**: Define a function called gt, which makes solid green triangles of whatever size we want.

Every contract has the	ee parts						
# gt::			Nı	umber			->Image
function name  Write some examples,				Domain			Range
examples:	then en ele ana i	abel What change	J				
•	4.0	\ • ·	. 7 (40	7		,	
gt(		) is <u>tr</u>	<u>langle(10,</u>	"solid",	"green" what th	) ne function produces	
gt(		) IS <u>tr</u>	tangle(20,	"50110",	what th	) ne function produces	_
end							
Write the definition, g	iving variable no	ames to all your in	put values				
fun at(		size	)•				
fun gt (		variable(s)					
triangle(size	solid".	"areen")					
_	, , , , , , , , , , , , , , , , , , , ,	g. co ,	what the funct	tion does with thos	se variable(s)		
end							
bc							
<b>Directions</b> : Define a	function called	he which make	es solid blue si	relec of what	over radius v	vo wont	
Directions: Define a	runction called	DC , WHICH MAKE	is solid blue cir	rcies oi whate	ever radius w	ve want.	
Every contract has thi	ree parts						
,							
# function name	:_			Domain			>
Write some examples	then circle and	lahel what change	<b>25</b>	Domain			Range
examples:	criori dii die di idi	abol What change	,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,,				
	(	input(s)	) is				
function nam	e	input(s)				what the function pro	duces
	(		) is				
function nam	e	input(s)				what the function pro	duces
end Write the definition, g	riving variable n	amos to all vour in	mut values				
vville the definition, g	iving variable no	anies to an your in	put values				
fun	(			):			
function	name	Va	ariable(s)				
_			what the funct	tion does with thos	e variable(s)		
end							

# Contracts, Examples & Definitions - Stars

### sticker

**Directions**: Define a function called sticker, which consumes a color and draws a 50px star of the given color.

	contract has three parts				
#	::				->
	function name	d labal what abaysas	Domain		Range
examp	some examples, then circle and	i iabei what changes			
Слапір	,				
	function name	input(s)	) is	what the function produces	
	ranction name			what the function produces	
-	function name	input(s)	) is	what the function produces	
end				·	
Write t	the definition, giving variable i	names to all your input va	lues		
fun	(		):		
	function name	variable(s)			
		wha	at the function does with those variable	(s)	
end					
goia	l-star				
Directi	cions: Define a function called	d gold-star, which ta	akes in a number and draws a	a solid gold star of that given size.	
F					
Every c	contract has three parts				
#	<u></u> :				
					->_
	function name	Llahal what changes	Domain		-> Range
Write s	some examples, then circle and	l label what changes	Domain		->Range
Write s	some examples, then circle and	l label what changes	Domain		->Range
Write s	some examples, then circle and ples:	,	Domain		->Range
Write s	some examples, then circle and	input(s)		what the function produces	->Range
Write s	some examples, then circle and ples:  ( function name	input(s)		·	->Range
Write s	some examples, then circle and ples:	input(s)	) is	what the function produces what the function produces	->Range
Write see examp	some examples, then circle and ples:  ( function name ( function name	input(s) input(s)	) is) is	·	->Range
Write see examp	some examples, then circle and ples:  ( function name	input(s) input(s)	) is) is	·	->Range
Write see examp	function name  function name  the definition, giving variable i	input(s) input(s) names to all your input va	) is) is	·	->Range
Write si examp	function name	input(s) input(s)	) is) is	·	->Range
Write s examp	function name  function name  the definition, giving variable i	input(s)  input(s)  names to all your input value (s)	) is) is	what the function produces	->Range

# Contracts, Examples & Definitions - Name

### name-color

**Directions**: Define a function called name-color, which makes an image of your name at size 50 in whatever color is given.

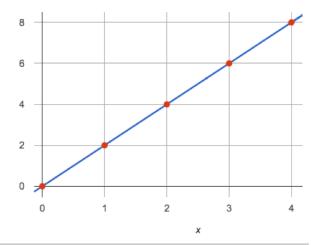
Every co	ontract has three part	'S					
#		::				->	
	function name			Domain			Range
Write so	ome examples, then c	ircle and label what cl	hanges				
examp	les:						
		,					
		(input(s)	) is		what the function produces		
	function name	input(s)			what the function produces		
		(	) <b>is</b>				
	function name	input(s)			what the function produces		
end							
Write th	ne definition, giving v	ariable names to all y	our input values				
		,					
fun	function name	(	variable(s)	):			
	Turiction name		variable(s)				
-			what the function	n does with those var	iable(s)		
end							
name	e-size						
паш	e-size						
Direction	ons: Define a function	on called name-siz	e, which makes an ir	nage of your na	me in your favorite color (be sure	to specify y	our name
	orite color!) in what		,	0 ,	,	. ,,	
anarav	orite color., in what	ever size is giveri.					
<b>-</b>							
Every co	ontract has three part	.S					
#						_	
#	function name	<del>-"</del>		Domain			Range
Write so		ircle and label what cl	hanges				
examp							
Схапірі							
		(	) is				
-	function name	input(s)	, .5		what the function produces		
		(	) is				
	function name	input(s)			what the function produces		
end							
Write th	ne definition, giving v	ariable names to all ye	our input values				
<b>c</b>		,		,			
fun	function name	(	variablo(s)	):			
	function name		variable(s)				
			what the function	does with those var	iable(s)		
end							

What's on your mind?				

# Notice and Wonder (Linearity)

### Part 1:

x	У
0	0
1	2
2	4
3	6
4	8



What do you Notice?	What do you Wonder?

### Part 2:

- What would be the next (x,y) pair for each of the tables?
- What would the y-value for each table be when x is 0?

x	У
0	
1	2
2	3
3	4
4	5
5	6

x	У
0	
1	20
2	17
3	14
4	11
5	8

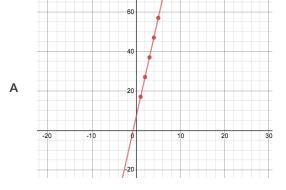
## Matching Tables to Graphs

For each of the tables below, find the graph that matches.

**Note:** Scales on the graphs vary. The tables are shown sideways to save space.

х	1	2	3	4	5
У	4	5	6	7	8

1



 x
 -5
 -4
 -3
 -2
 -1

 y
 5
 4
 3
 2
 1

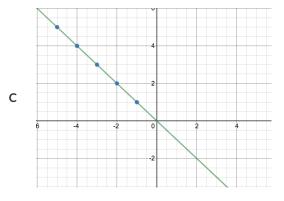
2

В	-5	5
	-10	

 x
 1
 2
 3
 4
 5

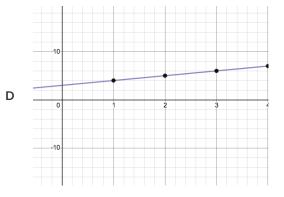
 y
 17
 27
 37
 47
 57

3



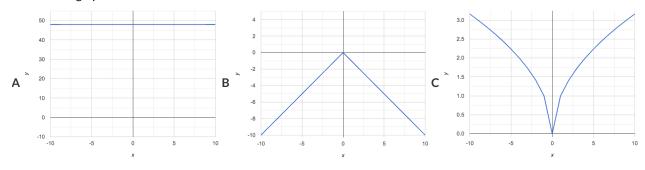
x -2 -1 0 1 2 y -6 -3 0 3 6

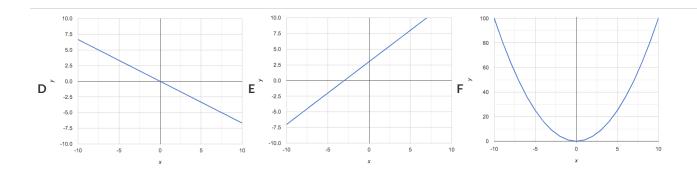
4



### Are All Graphs Linear?

If all linear relationships can be shown as points on a graph, does that mean all graphs are linear? Beneath each graph write **linear** or **not linear**.





What do you Notice?	What do you Wonder?

### Are All Tables Linear?

If all linear relationships can be shown as tables, does that mean all tables are linear? Look at the six tables shown below.

- 1) Extend as many of the tables as you can by adding the next (x,y) pair in the sequence.
- 2) If the table is linear, write down your prediction of what the y-value will be when x = 0.
- 3) If the table is not linear, write **not linear** instead of an answer for y.

Α						
х	-2	-1	0	1	2	
у	-2	-3	-4	-5	-6	

В						
x	2	3	4	5	6	
У	-12	-14	-16	-18	-20	

when x=0, y will equal С

х	2	3	4	5	6	
У	-12	-14	-16	-18	-20	

2 3 4 5 1 9 1 16 25 у

D						
x	5	6	7	8	9	
У	3	3	3	3	3	

when x=0, y will equal

when x=0, y will equal

when x=0, y will equal

Ε 2 3 1 4 5 Х 84 94 104 124 114

F						
х	-10	-9	-8	-7	-6	
У	$\frac{-1}{10}$	$\frac{-1}{9}$	$\frac{-1}{8}$	$\frac{-1}{7}$	$\frac{-1}{6}$	

when x=0, y will equal

when x=0, y will equal

What do you Notice?	What do you Wonder?

### Linear, Non-linear, or Bust?

Decide whether each representation is of a linear function, a non-linear function or is not a function at all! Remember: Functions will pass the Vertical Line Test!

 x
 y

 1
 5

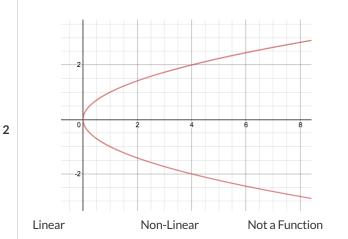
 2
 10

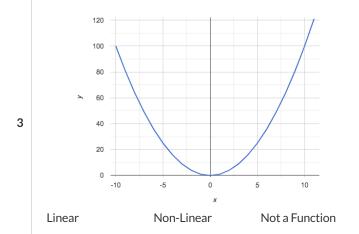
 3
 15

 4
 20

 5
 25

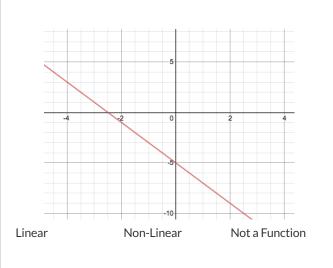
Linear Non-Linear Not a Function





x	У	
1	1	
2	4	
3	9	
4	16	
5	25	
6	36	
7	49	
Linear	Non-Linear	Not a Function

	x	У	
	1	1	
	2	2	
	3	3	
5	4	4	
	4	5	
	6	6	
	7	9	
	Linear	Non-Linear	Not a Function



### Slope & y-Intercept from Tables (Intro)

**slope (rate)**: how much y changes as x-increases by 1 **y-intercept**: the y-value when x = 0

x	-1	0	1	2	3	4
у	-1	1	3	5	7	9

1	Compu	to the	·lono:
1	) (.ombii	ite the s	sione:

- 2) Compute the y-intercept: \_\_
- 3) What strategies did you use to compute the slope and y-intercept?

The slope and y-intercept in this table are harder to find, because the x-values don't go up by 1 and we can't see a value for x=0. Try filling in the points that have been skipped to Compute the slope and y-intercept.

x	2	5	8	11
У	3	9	15	21

- 4) Compute the slope: 2
- 5) Compute the y-intercept:

The slope and y-intercept in this table are even harder to find, because the x-values are out of order! **Calculate the slope and y-intercept from** *any* **two points!** Be sure to show your work.

x	3	20	5	9	1
У	5	56	11	23	-1

- 6) Compute the slope:
- 7) Compute the y-intercept:

# Slope & y-Intercept from Tables (Practice)

х	-1	0	1	2	3	4
у	-1	2	5	8	11	14
1) slope:		·	y-intercept:	·		·
x	-2	-1	0	1	2	3
У	15	10	5	0	-5	-10
2) slope:			y-intercept:			
х	-3	-2	-1	0	1	2
у	-1	-0.5	0	0.5	1	1.5
2) alone:			v into			
3) slope:			y-intercept:			
	4		4			
Х	-1	0	1	2	3	4
У	-7	-3	1	5	9	13
4) slope:			v-intercept:			
, <u> </u>			<u> </u>			<u> </u>
x	-5	-4	-3	-2	-1	0
у	1	2.5	4	5.5	7	8.5
E) clone:	'	'	v intercent:			
3) slope.			y-intercept.			
х	-3	-2	-1	0	1	2
у	0	12.5	25	37.5	50	62.5
6) slope:			y-intercept:			
х	1	2	3	4	5	6
У	5	3	1	-1	-3	-5
7) slope:			y-intercept:			
х	-4	-2	0	2	4	6
у	0	4	8	12	16	20
		I	I		l l	

8) slope: \_\_\_\_\_\_ y-intercept: \_\_\_\_\_

# **Identifying Slope in Tables**

Can you identify the **slope** for the functions represented in each of these tables?

Note: Some tables may have their rows out of order!

	Х	у
	0	3
1	1	5
	2	7
	3	9

slope/rate:

	x	У
	-5	35
2	-4	28
	-3	21
	-2	14

slope/rate:

	Х	У
	12	15
3	13	15.5
	14	16
	16	17

slope/rate:

	х	У
	1	39
4	4	36
	3	37
	2	38

slope/rate:

	X	У
	13	57
5	9	41
	11	49
	7	33

slope/rate:

## Identifying Slope and y-intercept in Graphs

Can you identify the **slope** and **y-intercept** for each of these graphs? slope/rate: 1 y-intercept: slope/rate: 2 y-intercept: \_\_\_ slope/rate: 3 y-intercept: slope/rate: 4 y-intercept:

# Identifying Slope and y-intercept in Definitions

The following function definitions are written in math notation and in Pyret. Can you identify their **slope** and **y-intercept**?

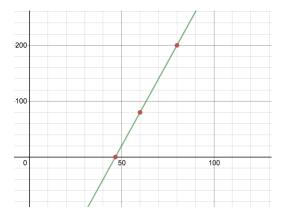
1	$f(x) = \frac{3}{4}x + 19$	slope/rate: y-intercept:
2	<b>fun</b> c(d) = (7.5 * d) + 22 <b>end</b>	slope/rate: y-intercept:
3	<b>fun</b> g(h): 20 - (16 * h) <b>end</b>	slope/rate: y-intercept:
4	g(x) = 91 + 4x	slope/rate: y-intercept:
5	<b>fun</b> i(j): -15 + (1.5 * j) <b>end</b>	slope/rate:
6	$h(x) = 10x - \frac{2}{5}$	slope/rate: y-intercept:

# Matching Graphs to Function Definitions

Match the function definitions to the graphs.

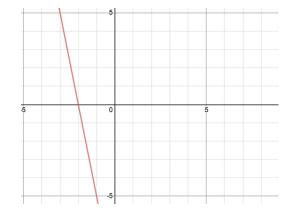
fun f(x): (-2/3 \* x) + 4 end 1

Α



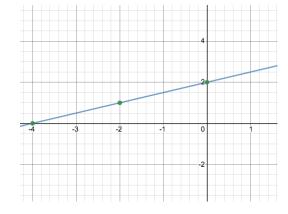
g(x) = 2x - 10 2

В



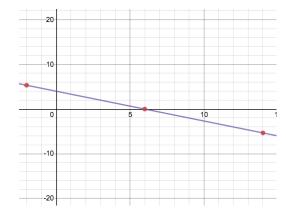
fun h(x): (0.5 \* x) + 2 end 3

С



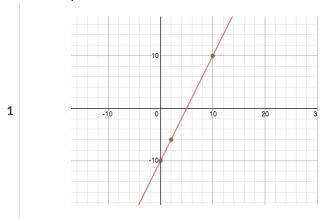
i(x) = 6x + -280 4

D

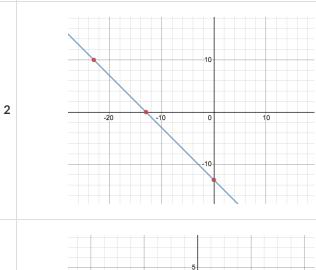


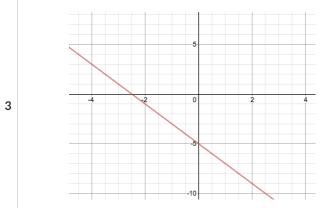
## Summarizing Graphs with Function Definitions

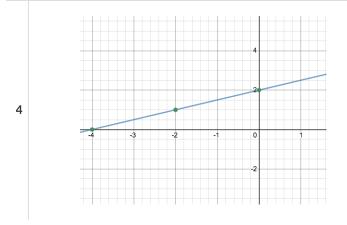
For each of the Graphs below, write the corresponding function definition, using both Pyret notation *and* function notation. The first one has been done for you.



fun f(x): 
$$(2 * x) - 10$$
 end  $f(x) = 2x - 10$ 







## Matching Tables to Function Definitions

Match each function definition to the corresponding table.

Note: The tables are shown sideways to save space.

fun	f(x)	: (-1	*	x )	end

fun 
$$f(x)$$
:  $x + 3$  end 2

fun 
$$f(x)$$
: 3 \* x end

**fun** 
$$f(x)$$
:  $(3 * x) - 5$  **end**

fun 
$$f(x)$$
: num-sqr(x) end 5

# **Summarizing Tables with Function Definitions**

For each of the Tables below, define corresponding function using Pyret code and function notation. We've started the first function out for you. (**Note:** The tables have been turned on their sides, to save space!)

1	х	0	1	2	3	4
1	У	-2	0	2	4	6
2	X	-2	-1	0	1	2
	У	-2	-1	0	1	2
3	x	-5	-4	-3	-2	-1
3	У	9	7	5	3	1
4	x	1	2	3	4	5
4	У	-1	-2	-3	-4	-5
5	x	9	10	11	12	13
5	У	14	16	18	20	22
	х	20	21	22	23	24
6	У	15	15.5	16	16.5	17

### **Solving Word Problems**

Being able to see functions as Contracts, Examples or Definitions is like having three powerful tools. These representations can be used together to solve word problems!

- 1) When reading a word problem, the first step is to figure out the **Contract** for the function you want to build. Remember, a Contract must include the Name, Domain and Range for the function!
- 2) Then we write a **Purpose Statement**, which is a short note that tells us what the function *should do*. Professional programmers work hard to write good purpose statements, so that other people can understand the code they wrote!
- 3) Next, we write at least two **Examples**. These are lines of code that show what the function should do for a *specific* input. Once we see examples of at least two inputs, we can *find a pattern* and see which parts are changing and which parts aren't.
- 4) To finish the Examples, we circle the parts that are changing, and label them with a short variable name that explains what they do.
- 5) Finally, we **define the function** itself! This is pretty easy after you have some examples to work from: we copy everything that didn't change, and replace the changeable stuff with the variable name!

# Matching Word Problems and Purpose Statements

Match each word problem below to its corresponding purpose statement.

Alejahul o wili have to clean up depending off how moch text has eaten.	Alejandro's rabbit, Rex, poops about 1/5 of what it eats. His rabbit hutch is  10 cubic feet. Write a function to figure out how much rabbit poop  3 C Consume the pounds of food Rex eats and multiply by 5.	Adrienne's raccoon, Rex, eats 5 more pounds of food each week than her pet squirrel, Lili, who is 7 years older. Write a function to determine how <b>2</b> B Consume the pounds of food Rex eats and subtract 5. much Lili eats in a week, given how much Rex eats.	Annie got a new dog, Xavier, that eats about 5 times as much as her little dog, Rex, who is 10 years old. She hasn't gotten used to buying enough dogfood for the household yet. Write a function that generates an setimate for how many pounds of food Xavier will eat, given the amount of food that Rex usually consumes in the same amount of time.
---	---	--	--

# Writing Examples from Purpose Statements

We've provided contracts and purpose statements to describe two different functions. Write examples for each of those functions.

Contract and Purpose S	tatement						
Every contract has three p	arts						
# triple:			I	Number			->Number
function name				Domain			Range
# Consumes a Number	r and ti	riples it					
Examples			wnat	does the function do?			
Write some examples, the	n circle and	label what ch	nanges				
examples:							
	(		) is				
function name		input(s)			W	hat the function produces	
	(		) is				
function name end	.,	input(s)			W	hat the function produces	
Contract and Purpose S	tatement						
Every contract has three p	arts						
# uncide_down.				Image			->Image
# upside-down::				Domain			Range
# Consumes an image	e, and t	urns it	upside down	n by rotating	it 180	) degrees.	
	•		what	does the function do?			
Examples							
Write some examples, the	n circle and	label what ch	nanges				
examples:							
	(			) is			
function name		i	nput(s)			what the function p	roduces
	(			) is			
function name		input(	(s)			what the function produc	ces

end

# Fixing Purpose Statements

Beneath each of the word problems below is a purpose statement that is either missing information or includes unnecessary information. Write an improved version of each purpose statement beneath the original.

1) <b>Word Problem:</b> The New York City ferry costs \$2.75 per ride. The Earth School requires two chaperones for any field trip. Write a function fare that takes in the number of students in the class and returns the total fare for the students and chaperones. <b>Purpose Statement:</b> Define a function fare to take in the number of students and add 2. <b>Improved Purpose Statement:</b>
2) <b>Word Problem:</b> It is tradition for the Green Machines to go to Humpy Dumpty's for ice cream with their families after their soccer games. Write a function cones to take in the number of kids and calculate the total bill for the team, assuming that each kid brings two family members and cones cost \$1.25.
<b>Purpose Statement:</b> Define a function cones to take in the number of kids on the team and multiply it by 1.25. <b>Improved Purpose Statement:</b>
3) <b>Word Problem</b> : The cost of renting an ebike is \$3 plus an additional \$0.12 per minute. Write a function ebike that will calculate the cost of a ride, given the number of minutes ridden. <b>Purpose Statement</b> : Define a function ebike to take in the number of minutes and multiply it by 3.12. <b>Improved Purpose Statement</b> :
4) Word Problem: Suleika is a skilled house painter at only age 21. She has painted hundreds of rooms and can paint about 175 square feet an hour. Write a function paint that takes in the number of square feet of the job and calculates how many hours it will take her.  Purpose Statement: Define a function paint to take in the number of square feet of walls in a house and divide them by 175 to calculate the number of hours that it will take 21 year-old Suleika to complete the paint job.  Improved Purpose Statement:

# Word Problem: rocket-height

**Directions**: A rocket blasts off, and is now traveling at a constant velocity of 7 meters per second. Use the Design Recipe to write a function rocket-height, which takes in a number of seconds and calculates the height.

Contract and Purpose Statemer	nt					
Every contract has three parts						
<u>#</u> .::					->	-
function name			Domain			Range
<u>#</u>		what does the	function do?			
Examples		at does the				
Write some examples, then circle a	and label what change	es				
examples:						
(		) <b>is</b>				
function name	input(s)			what the function produces		
(		) is				
function name end	input(s)			what the function produces		
Definition						
Write the definition, giving variable	e names to all your in	put values				
fun (			١.			
function name	varia	ble(s)				
end		what the function doe	es with those variable(	(s)		

# Danger and Target Movement

**Directions**: Use the Design Recipe to write a function update-danger, which takes in the danger's x- and y-coordinate and produces the next x-coordinate, which is 50 pixels to the left.

# ::	
	ange
# what does the function do?	
Examples	
Write some examples, then circle and label what changes	
examples:	
() is	
function name input(s) what the function produces	_
function name input(s) input(s) what the function produces	
end what the function produces	
Definition	
Write the definition, giving variable names to all your input values	
fun(	
function name variable(s)	
what the function does with those variable(s)	
end	
Contract and Purpose Statement	
Every contract has three parts	
Every contract has three parts	
Every contract has three parts  # :: ->	ange
Every contract has three parts  # :: ->	ange
Every contract has three parts  # :: ->	ange
Every contract has three parts  # :: -> function name Domain Ro  # what does the function do?  Examples	ange
Every contract has three parts  # :: ->	ange
# ::	ange
# ::	ange
# ::	ange
Every contract has three parts  # ::	ange
# ::	ange
Every contract has three parts  # ::	ange
Every contract has three parts  # ::	ange
Every contract has three parts  # ::	ange

end

# Surface Area of a Rectangular Prism - Explore 1) What do you picture in your mind when you hear rectangular prism? 2) What do you picture in your mind when you hear surface area? 3) Open the Surface Area of a Rectangular Prism Starter File and click "Run". 4) Type prism into the Interactions Area and hit "enter" to see an image of a rectangular prism. What do you notice about the image? 5) How many faces does this prism have? Find PART 1 in the starter file. You will see a definition for front and back. 6) How did the author know to use width and height as the dimensions for front and back? 7) Why are front and back defined to be the same thing? 8) Add definitions for the other faces of the prism, using these definitions as a model, and the image of the prism as a support. Find PART 2 in the starter file. You'll see a list that only includes front and back . 9) Complete the faces list, then type print-imgs (faces) into the interactions area. What do you see? We're going to print the faces following directions in PART 3 and build a paper model of a rectangular prism. Before you print and build your prism, you can change the length, width, and height of your prism at the top of the starter file. Be sure that all 3 dimensions are different, and that they are all small enough to fit on a sheet of paper. If you change them, record your new dimensions here. LENGTH: \_\_\_\_\_ HEIGHT: \_\_\_\_ 12) Calculate the surface area of your prism, by adding the area of each face. \_\_\_\_\_ Show your work below.

### **Problem Decomposition**

- Sometimes a problem is too complicated to solve all at once. Maybe there are too many variables, or there is just so much information that we can't get a handle on it!
- We can use **Problem Decomposition** to break those problems down into simpler pieces, and then work with the pieces to solve the whole. There are two strategies we can use for decomposition:
  - **Top-Down** Start with the "big picture", writing functions or equations that describe the connections between parts of the problem. Then, work on defining those parts.
  - **Bottom-Up** Start with the smaller parts, writing functions or equations that describe the parts we understand. Then, connect those parts together to solve the whole problem.
- You may find that one strategy works better for some types of problems than another, so make sure you're comfortable using either one!

# Word Problems: revenue, cost

**Directions**: Use the Design Recipe to write a function revenue, which takes in the number of glasses sold at \$1.75 apiece and calculates the total revenue.

Cont	ract and Purpose	Statemen <u>t</u>						
Every	contract has three	parts						
#		::					->	
	function name				Domain			Range
#				what da	es the function do?			
Exam	nples			what doe	es the function do:			
	some examples, the	en circle and	l label what char	nges				
examp	les:							
		(		) <b>is</b>				
	function name	<u></u>	input(s)			what the function produces		
	function name	(	input(s)	) is		what the function produces		
end	function name		input(s)			what the function produces		
Defir	nition							
Writet	he definition, givir	ng variable r	ames to all your	input values				
fun		(			):			
	function name		va	ariable(s)				
					on does with those var	:-bl-/-)		
end				what the function	on does with those var	lable(s)		
Cont	ract and Purpose	Statement	_		_			
	contract has three							
							->	
<u>#</u>	function name	<del></del>			Domain		^	Range
#								
Exam					es the function do?			
	some examples, the	en circle and	l label what char	nges				
examp		0 0 00 0	. 145 51 11114 51141	.800				
		(		) <b>is</b>				
	function name		input(s)			what the function produces		
		(		) is				
end	function name		input(s)			what the function produces		
Defir	nition							
	he definition, givir	ng variable r	ames to all your	input values				
fun		(			).			
	function name		va	ariable(s)				
				what the function	on does with those var	riable(s)		

end

# Word Problem: profit

**Directions**: Use the Design Recipe to write a function profit that calculates total profit from glasses sold, which is computed by subtracting the total cost from the total revenue.

Contract and Purpose Stateme	ent					
Every contract has three parts						
# ::					->	
function name			Domain		Range	
#						
Examples		what does the	function do?			
Write some examples, then circle	and label what chang	ges				
examples:						
(		) <b>is</b>				
function name	input(s)			what the function produces		
(		) is				
function name end	input(s)			what the function produces		
Definition						
Write the definition, giving varial	ole names to all your i	nput values				
fun	(		).			
function name	vari	able(s)				
and		what the function do	es with those variable(s)			

### Profit - More than one Way!

Four students defined the same revenue and cost functions, shown below: fun revenue(g): 1.75 \* g end fun cost(g): 0.3 \* g end However, they came up with four different definitions for profit: Khalil: **fun** profit(g): (1.75 \* g) - (0.3 \* g) **end** Samaria: fun profit(g): (1.75 - 0.3) \* g endAlenka: fun profit(g): 1.45 \* g end Fauzi: fun profit(g): revenue(g) - cost(g) end 1) Which of these four definitions do you think is "best", and why? 2) If lemons get more expensive, which definitions of profit need to be changed? 3) If Sally raises her prices, which definitions of profit need to be changed? 4) Which definition of profit is the most flexible? Why?

### Top Down or Bottom Up

Jamal's trip requires him to drive 20mi to the airport, fly 2,300mi, and then take a bus 6mi to his hotel. His average speed driving to the airport is 40mph, the average speed of an airplane is 575mph, and the average speed of his bus is 15mph.

Aside from time waiting for the plane or bus, how long is Jamal in transit?

Bear's Strategy:	Lion's Strategy:
$DriveTime = 20miles \times \frac{1hour}{40miles} = 0.5hours$	InTransitTime = DriveTime + FlyTime + BusTime
$FlyTime = 2300miles \times \frac{1hour}{575miles} = 4hours$	$DriveTime = 20miles \times \frac{1hour}{40miles} = 0.5hours$
$BusTime = 6miles \times \frac{1hour}{15miles} = 0.4hours$	$FlyTime = 2300miles \times \frac{1hour}{575miles} = 4hours$
InTransitTime = DriveTime + FlyTime + BusTime	$BusTime = 6miles \times \frac{1 hour}{15miles} = 0.4 hours$
0.5 + 4 + 0.4 = 4.9 hours	0.5 + 4 + 0.4 = 4.9 hours

<sup>1)</sup> Whose Strategy was Top Down? How do you know?

- 2) Whose Strategy was Bottom Up? How do you know?
- 3) Which way of thinking about the problem makes more sense to you?

What's happening with that Math?!

When calculating Jamal's drive time, we multiplied distance by speed. More specifically, we multiplied the starting value (20miles) by  $\frac{1 \, hour}{40miles}$ . Why? Why not reverse it, to use  $\frac{40miles}{1 \, hour}$ , as stated in the problem?

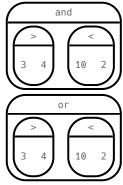
Time is the desired outcome. Looking at the units, we can see that speed must have miles as its denominator to cancel out the miles in the starting value.

$$\frac{20mi}{1} \times \frac{1hour}{40miles} = \frac{20 \text{ miles} \times 1hour}{40 \text{ miles}} = \frac{20}{40}hour = \frac{1}{2}hour$$

91

### Inequalities

- Sometimes we want to *ask questions* about data. For example, is x greater than y? Is one string equal to another? These questions can't be answered with **Numbers**. Instead, they are answered with a new data type called a **Boolean**.
- video games use Booleans for many things: asking when a player's health is equal to zero, whether two characters are close enough to bump into one another, or if a character's coordinates put it off the edge of the screen.
- A Boolean value is either true or false. Unlike Numbers, Strings, and Images, Booleans have only two possible values.
- You already know some functions that produce Booleans, such as < and >! Our programming language has them, too: 3 < 4,</li>
   10 > 2, and -10 == 19.
- We also have ways of writing Compound Inequalities, so we can ask more complicated questions using the and or functions.
  - (3 > 4) **and** (10 < 2) translates to "three is greater than four *and* ten is less than two". This will evaluate to **false**, since the **and** function requires that both sub-expressions be **true**.
  - (3 > 4) **or** (10 < 2), which translates to "three is greater than four *or* ten is less than two". This will evaluate to **true**, since the **or** function only requires that one sub-expression be **true**.
- The Circles of Evaluation work the same way with Booleans that they do with Numbers, Strings and Images:



Boolean Functions
Explore the functions in the <u>Boolean Starter File</u> .
Fill in the blanks below so that each of the five functions returns true
<b>1)</b> is-odd()
2) is-even()
3) is-less-than-one()
<b>4)</b> is-continent()
5) is-primary-color()
Fill in the blanks below so that each of the five functions returns false
<b>6)</b> is-odd()
7) is-even()
8) is-less-than-one()
9) is-continent()
<b>10)</b> is-primary-color()

## Simple Inequalities

Each inequality expression in the first column contains a number.

Decide whether or not that number is a solution to the expression and place it in the appropriate column.

Then identify 4 solution and 4 non-solution values for X.

- Solutions will make the expression true.
- Non-Solutions will make the expression false .

Challenge yourself to use negatives, positives, fractions, decimals, etc. for your x values.

	Expression	4 solutions that evaluate to <b>true</b>	4 non-solutions that evaluate to <b>false</b>					
а	x > 2							
b	x <= -2							
С	x < 3.5							
d	x >= -1							
е	x > -4							
f	x <> 2							
1) For	I) For which inequalities was the number from the expression part of the solution?							

_	I OI WINCH	i ii ieuuaii lies w	as the numb	.c.	XDI 63310111101	part of the solution?

- 3) For which inequalities were the solutions on the left end of the number line?
- 4) For which inequalities were the solutions on the right end of the number line?

# Converting Circles of Evaluation to Code

For each Circle of Evaluation on the left-hand side, write the Code for the Circle on the right-hand side

	Circle of Evaluation	Code
1	+ 9 4 5	
2	and < < < 10 15	
3	or  == == yum "banana"	
4	>= String-length "My Game"	
5	and and c c c c l x s l l l l l l l l l l l l l l l l l	

# Compound Inequalities — Practice

create the Circles of Evaluation, their convert the expressions into Code in the space provided.
1) 2 is less than 5, and 0 is equal to 6
What will this evaluate to?
2) 6 is greater than 8, or -4 is less than 1
What will this evaluate to?
3) The String "purple" is the same as the String "blue", and 3 plus 5 equals 8
What will this evaluate to?
4) Write the contracts for <b>and</b> & <b>or</b> in your Contracts page.

### Compound Inequalities: Solutions & Non-Solutions

For each Compound Inequality listed below, identify 4 solutions and 4 non-solutions.

If there are **no solutions** or the solution set includes **all real numbers**, write that instead of making a list.

- Solutions for intersections, which use and will make both of the expressions true.
- Solutions for unions, which use **or** will make at least one of the expressions **true**.

Pay special attention to the numbers in the sample expression! Challenge yourself to use negatives, positives, fractions, decimals, etc. for your x values.

The first two have been done for you - Answers will vary!

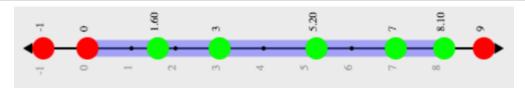
	Everession	A colutions that avaluate to true	4 non-solutions that evaluate to false
	Expression	4 solutions that evaluate to true	4 non-solutions that evaluate to Tatse
а	x > 5 and $x < 15$	6, 9.5, 12, 14.9	-2, 5, 15, 16.1
b	x > 5  or  x < 15	All real numbers	No non-solutions
С	$x \le -2$ and $x > 7$		
d	x <= -2  or  x > 7		
е	x < 3.5  and  x > -4		
f	x < 3.5  or  x > -4		
g	$x \ge -1$ and $x \ge -5$		
h	$x \ge -1 \text{ or } x > -5$		
i	x < -4 and $x > 2$		

1	) Could there ev	er he a union	with no s	olutions? F	volain vour	thinking
т	<i>i</i> Could there ev	er be a uriior	1 991111 110 5	OIULIONS : E	XDIAIII VOUL	LI III IKII 12.

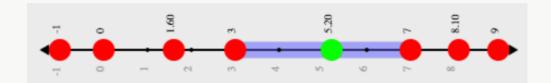
2) Could there ever be an intersection whose solution is *all real numbers*? Explain your thinking.

## **Compound Inequality Functions**

Each of the plots below was generated using the code inequality (comp-ineq, [list: -1, 0, 1.6, 3, 5.2, 7, 8.1, 9]). Using the numbers 3 and 7, write the code to define comp-ineq for each plot. Note: The example is defined using 0 and 8.1 rather than 3 and 7.



code: fun comp-ineq(x): (x > 0) and  $(x \le 8.1)$  end



code:



code:



code:



code:

### Sam the Butterfly

Open the Sam the Butterfly Starter File starter file and click "Run". (Hi, Sam!)

Move Sam around the screen using the arrow keys.

1) What do you Notice about the program?

2) What do you Wonder?

3) What do you see when Sam is at (0,0)? Why is that?

4) What changes as the butterfly moves left and right?

Sam is in a 640 × 480 yard. Sam's mom wants Sam to stay in sight. How far to the left and right can Sam go and still remain visible?

Use the new inequality functions to answer the following questions with code:

5) Sam hasn't gone off the left edge of the screen as long as...

6) Sam hasn't gone off the right edge of the screen as long as...

7) Use the space below to draw Circles of Evaluation for these two expressions:

# Left and Right

**Directions**: Use the Design Recipe to write a function is-safe-left, which takes in an x-coordinate and checks to see if it is greater than -50.

Cont	tract and Purpose	Statemen <u>t</u>						
Every	contract has three	parts						
#		::					->	
	function name				Domain			Range
#				what do	es the function do?			
Exan	nples			wnat doe	es the function do:			
	some examples, the	en circle and	l label what char	nges				
examp								
		(		) is				
	function name	<u> </u>	input(s)			what the function produces		
	function name	(	input(s)	) is		what the function produces		
end	Tuncuoti Haine		mpat(s)			what the function produces		
Defi	nition							
Write	the definition, givir	ng variable r	names to all your	input values				
fun		(			):			
	function name		Vi	ariable(s)	<del></del>			
						-:bl-/-)		
end				what the function	on does with those var	i ianic(2)		
	tract and Purpose							
∟very	contract has three	parts						
#	function name	::			Domain		>	Range
ш	Turicuon name				Domain			Range
#					es the function do?			
	nples							
	some examples, the	en circle and	d label what char	nges				
examp	nes:							
	function name	(	input(s)	) is		what the function produces		
		,	20(0)	) is		III III IIII produces		
	function name	(	input(s)			what the function produces		
end								
	nition the definition givin	ng variable :	amos to all vers	input values				
	the definition, givir	ig var labie r	iames to all your	iriput values				
fun _	function name	(	V	ariable(s)	):			
			•					
				what the function	on does with those var	riable(s)		

end

## Word Problem: is-onscreen

**Directions**: Use the Design Recipe to write a function is-onscreen, which takes in an x- and y-coordinate, and checks to see if Sam is safe on the left while also being safe on the right.

Contract and Purpose Statemer	nt					
Every contract has three parts						
<u>#</u> .::					->	-
function name			Domain			Range
<u>#</u>		what does the	function do?			
Examples		at does the				
Write some examples, then circle a	and label what change	es				
examples:						
(		) <b>is</b>				
function name	input(s)			what the function produces		
(		) is				
function name end	input(s)			what the function produces	<del>-</del>	
Definition						
Write the definition, giving variable	e names to all your in	put values				
fun (			١٠			
function name	varia	ble(s)				
end		what the function doe	es with those variable(	(s)		

### **Piecewise Functions**

- Sometimes we want to build functions that act differently for different inputs. For example, suppose a business charges \$10/pizza, but only \$5 for orders of six or more. How could we write a function that computes the total price based on the number of pizzas?
- In math, **Piecewise Functions** are functions that can behave one way for part of their Domain, and another way for a different part. In our pizza example, our function would act like cost(pizzas) = 10 \* pizzas for anywhere from 1-5 pizzas. But after 5, it acts like cost(pizzas) = 5 \* pizzas.
- Piecewise functions are divided into "pieces". Each piece is divided into two parts:
  - 1. How the function should behave
  - 2. The domain where it behaves that way
- Our programming language can be used to write piecewise functions, too! Just as in math, each piece has two parts:

```
fun cost(pizzas):
   if pizzas < 6: 10 * pizzas
   else if pizzas >= 6: 5 * pizzas
   end
end
```

Piecewise functions are powerful, and let us solve more complex problems. We can use piecewise functions in a video game to add or subtract from a character's x-coordinate, moving it left or right depending on which key was pressed.

# Red Shape - Explore

1) Open the Red Shape Starter File, and read through the code you find there. This code contains new programming that you haven't seen yet! Take a moment to list everything you Notice, and then everything you Wonder...

Notice	Wonder
2) What happens if you click "Run" and type red-shape("ellipse	') ?
3) Add another example for "triangle".	
4) Add another line of code to the definition, to define what the functio	n should do with the input "triangle".
5) Come up with some new shapes, and add them to the code. Make sur	re you include examples or you will get an error message!
6) In your own words, describe how <i>piecewise functions</i> work in this pro	ogramming environment.

## Word Problem: red-shape

**Directions**: A friend loves red shapes so we've decided to write a program that makes it easy to generate them. Write a function called red-shape which takes in the name of a shape and makes a 20-pixel, solid, red image of the shape.

Contract and Purpose Statement		
Every contract has three parts		
# red-shape::	String Domain	-> <i>Image</i> Range
# Given a shape name, produc	re a solid, red, 20-pixel image of the shape.  what does the function do?	
Examples		
Write some examples, then circle and lab <b>examples:</b>	el what changes	
•	) is circle(20, "solid", "red")  what the function produces	
	) is <pre>triangle(20, "solid", "red")</pre>	
	) <b>is</b> star(20, "solid", "red") what the function produces what the function produces	
end Definition		_
Write the definition, giving variable name	es to all your input values	
	variable(s)	
ifelse if	:	
else if	:	
	; 	
else: end		

end

# Word Problem: update-player

**Directions**: The player moves up and down by 20 pixels each time. Write a function called update-player, which takes in the player's x- and y-coordinate and the name of the key pressed ("up" or "down"), and returns the new y-coordinate.

Contract and Purpose Statement			
Every contract has three parts			
# ::			->
function name	Domain		Range
#			
Examples	what does the function do?		
Write some examples, then circle and label what chan	iges		
examples:	,gco		
•			
<pre>update-player( 100, 200, "up" ) is function name</pre>		what the function produces	
(	) <b>is</b>		
function name input(s)		what the function produces	
(	) is		
function name input(s)		what the function produces	
	) is		
function name input(s) end		what the function produces	
Definition			
Write the definition, giving variable names to all your	input values		
fun (	):		
	riable(s)		
	what the function does with those variable	e(s)	
	what the function does with those variable	e(s)	
	what the function does with those variable	e(s)	
	what the function does with those variable	e(s)	

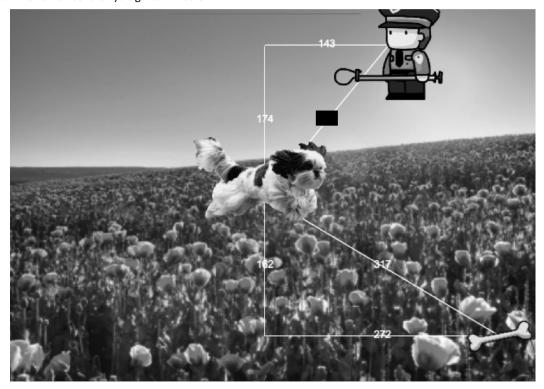
end

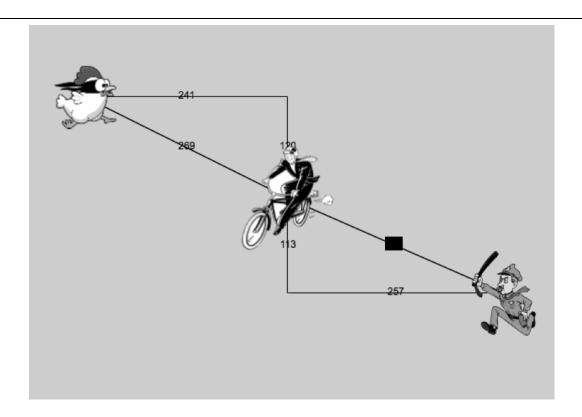
# Challenges for update-player

or each of the challenges below, see if you can come up with two EXAMPLES of now it should work! L) <b>Warping</b> - Program one key to "warp" the player to a set location, such as the center of the screen.
examples:
update-player(,,) is
update-player(,,) is
2) <b>Boundaries</b> - Change update-player such that PLAYER cannot move off the top or bottom of the screen.
examples:
update-player(,,) is
update-player(,,) is
B) Wrapping - Add code to update-player such that when PLAYER moves to the top of the screen, it reappears at the bottom, and vice versa.
examples:
update-player(,) is
update-player(,,) is
H) <b>Hiding</b> - Add a key that will make PLAYER seem to disappear, and reappear when the same key is pressed again.
examples:
update-player(,,) is
update-player(,) is

### Writing Code to Calculate Missing Lengths

In each of the game screenshots below, one of the distance labels has been hidden. Write the code to generate the missing distance on the line below each image. Hint: Remember the Pythagorean Theorem!

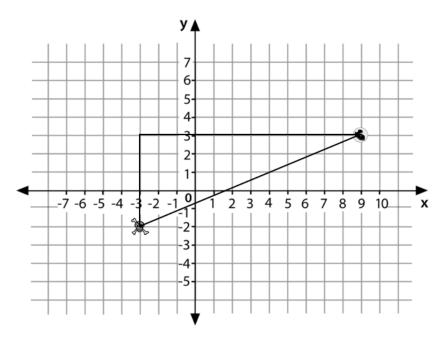




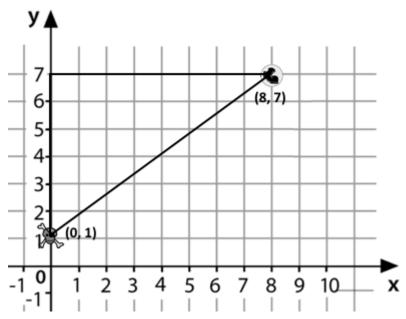
#### Distance on the Coordinate Plane

Distance between the pyret and the boot:

num-sqrt(num-sqr(line-length(9, -3)) + num-sqr(line-length(3, -2)))



Explain how the code works.



Now write the code to find the distance between this boot and pyret.

#### Circles of Evaluation: Distance between (0, 2) and (4, 5)

The distance between  $x_1$  and  $x_2$  is computed by line-length(x1, x2). The distance between  $y_1$  and  $y_2$  is computed by line-length(y1, y2). Below is the equation to compute the hypotenuse of a right triangle with those amount for legs:

$$\sqrt{line-length(x_2,x_1)^2 + line-length(y_2,y_1)^2}$$

Suppose your player is at (0, 2) and a character is at (4, 5). What is the distance between them?

**1.** Identify the values of  $x_1$ ,  $y_1$ ,  $x_2$ , and  $y_2$ 

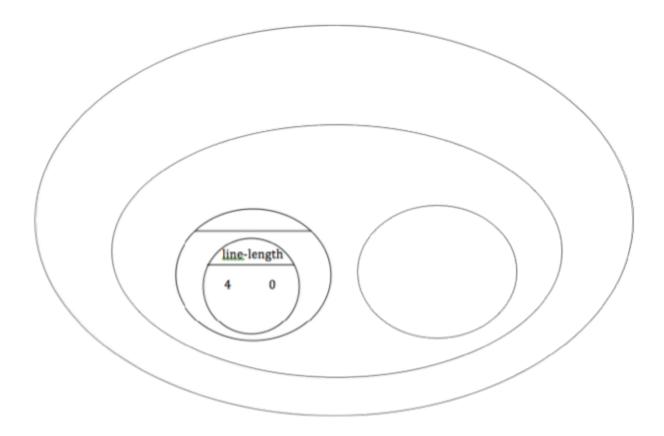
<i>x</i> 1	<i>y</i> 1	<i>x</i> 2	<i>y</i> 2
(x-value of 1st point)	(y-value of 1st point)	(x-value of 2nd point)	(y-value of 2nd point)

The equation to compute the distance between these points is:

$$\sqrt{line-length(4,0)^2 + line-length(5,2)^2}$$

2. Translate the expression above, for (0,2) and (4,5) into a Circle of Evaluation below.

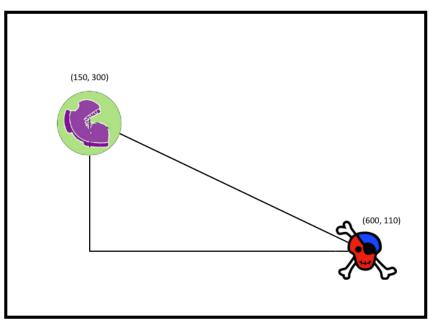
Hint: In our programming language num-sqr is used for  $x^2$  and num-sqrt is used for  $\sqrt{x}$ 



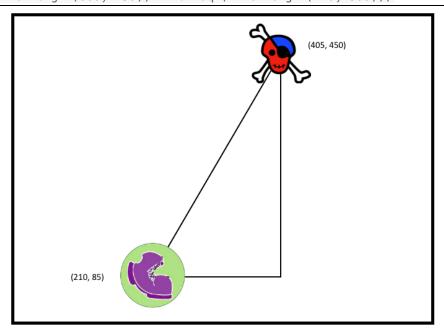
3. Convert the Circle of Evaluation to Code below.

#### **Distance From Game Coordinates**

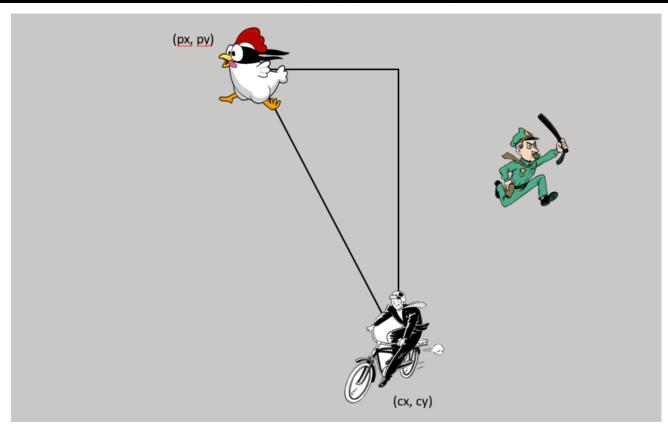
For each of the game screenshots, write the code to calculate the distance between the indicated characters. *The first one has been done for you.* 



num-sqrt(num-sqr(line-length(600, 150)) + num-sqr(line-length(110, 300)))



### Distance (px, py) to (cx, cy)



**Directions**: Use the Design Recipe to write a function distance, which takes in FOUR inputs: px and py (the x- and y-coordinate of the Player) and cx and cy (the x- and y-coordinates of another character), and produces the distance between them in pixels.

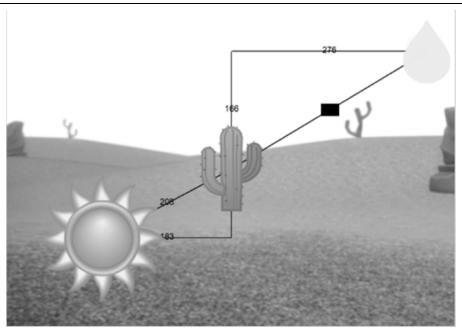
Contract and Purpose Stateme	ent		
Every contract has three parts			
# ::		Domain	->Range
#		Domain	Kange
	what doe	es the function do?	
Examples			
Write some examples, then circle examples:	and label what changes		
	) is	what the function p	produces
(	) is		
function name end	input(s)	what the function p	produces
Definition			
Write the definition, giving varial	ole names to all your input values		
funfunction_name	(	):	
ranction fiame	vai iauie(s)		
	what the function	on does with those variable(s)	

112

end

#### Comparing Code: Finding Missing Distances

For each of the game screenshots below, the math and the code for computing the covered distance is shown. Notice what is similar and what is different about how the top and bottom distances are calculated. Think about why those similarities and differences exist and record your thinking.



$$\sqrt{166^2 + 276^2}$$

num-sqrt(num-sqr(166) + num-sqr(276))

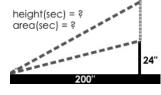


$$\sqrt{276^2 - 194^2}$$

num-sqrt(num-sqr(276) - num-sqr(194))

#### Top Down/Bottom Up

A retractable flag pole starts out 24 inches tall, and grows taller at a rate of 0.6in/sec. An elastic is anchored 200 inches from the base and attached to the top of the pole, forming a right triangle. Using a top-down or bottom-up strategy, define functions that compute the *height* of the pole and the *area* of the triangle after a given number of seconds.



#	::					->	
	function name			Domain		<del></del>	Range
4							
#			what does	the function do?			
exam	nles:		What does	the function do.			
Oztaiii,	J. 63.						
	(		) is				
	function name	input(s)			what the function produces		
	,		٠.				
	function name	input(s)	) is		what the function produces		
end	Tunction hame	input(s)			what the function produces		
enu							
fun	(			١٠			
- Iuii _	function name	varia	ble(s)				
			what the function	does with those variab	le(s)		
end							
ш							
#	function name			Domain		>	Range
	ranction name			Domain			range
#							
			what does	the function do?			
exam	ples:						
	(		) is				
	function name	input(s)			what the function produces		
	(		) is				
	function name	input(s)	/ is		what the function produces		
end							
3114							
fun	(			):			
	function name	varia	ble(s)				

what the function does with those variable(s)

end

114

### Word Problem: is-collision

**Directions**: Use the Design Recipe to write a function is-collision, which takes in FOUR inputs: px and py (the x- and y-coordinate of the Player) and cx and cy (the x- and y-coordinates of another character), and checks if they are close enough to collide.

Contra	ct and Purpose Stateme	nt					
Every co	ntract has three parts						
#	<u> </u>					>	
	function name			Domain			Range
#							
Examp	les		what does the	function do?			
Write so	me examples, then circle	and label what chan	ges				
example	s:						
	(		) is				
	function name	input(s)			what the function produces		
	(		) is				
end	function name	input(s)			what the function produces		
Definit	ion						
Write the	e definition, giving variab	e names to all your i	nput values				
fun	(			):			
	function name	var	iable(s)	<u>-</u>			
end			what the function doe	es with those variable(s	)		

takes four inputs (two Numbers and two Strings), and it evaluates to an Image . From the contract, we know ellipse (100, 50, "outline", "red") will evaluate to an Contracts tell us how to use a function. For example: ellipse :: (Number, Number, String) -> Image tells us that the name of the function is ellipse; it Image.

Name		Domain		Range
# num-sqr	••	Number	V	Number
num-sqr(9)				
# num-sqrt	::	Number	\ \	Number
num-sqrt(25)				
# string-length :	::	String	\ \	Number
string-length("Rainbow")				
# string-contains :	::	String, String	\ \	Boolean
string-contains("catnap", "cat")				
# triangle :	::	Number, String, String	\ \	Image
triangle(80, "solid", "darkgreen")	1")			
# star :	::		\ \	
# circle :	::		\ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \ \	
# square :	::		\	
<pre># rectangle :</pre>	::		\ \ \	

takes four inputs (two Numbers and two Strings), and it evaluates to an Image . From the contract, we know ellipse (50, 100, "solid", "teal") will evaluate to an Image . Contracts tell us how to use a function. For example: ellipse :: (Number, Number, String) -> Image tells us that the name of the function is ellipse; it

<pre># triangle-sas</pre>	# star-polygon	# radial-star	# isosceles-triangle	<pre># right-triangle</pre>	# regular-polygon	# text	# ellipse	Name # rhombus
								Domain
<b>\</b>	V	<b>\</b>	\ <u>\</u>	\ <u>\</u>	<b>\</b>	V	V	Range

takes four inputs (two Numbers and two Strings), and it evaluates to an Image . From the contract, we know ellipse (100, 50, "solid", "fuchsia") will evaluate to an Contracts tell us how to use a function. For example: ellipse :: (Number, Number, String) -> Image tells us that the name of the function is ellipse, it Image

Image.		
Name	Domain	Range
# triangle-asa		\ \ \
# image-url		\ \ 
# scale		\ \ \
# rotate		\ \ \
# overlay		V
# put-image		\ \ \
<pre># flip-horizontal</pre>		\ \ \
# flip-vertical		V
# above		V

takes four inputs (two Numbers and two Strings), and it evaluates to an Image . From the contract, we know ellipse (100, 50, "outline", "darkgreen") will evaluate to an Contracts tell us how to use a function. For example: ellipse :: (Number, Number, String, String) -> Image tells us that the name of the function is ellipse, it

*	<b>‡</b>	# #	#	# #	#	##	#	# #	#	# #	# and :	# Or :::	<pre># beside :::</pre>	Name Domain	Image.
		· V		<u>'</u>		->		<b>!</b>		<b>!</b>	- - -	\ \ \	ľ	Range	



These materials were developed partly through support of the National Science Foundation, (awards 1042210, 1535276, 1648684, and 1738598), and are licensed under a Creative Commons 4.0 Unported License. Based on a work at www.BootstrapWorld.org. Permissions beyond the scope of this license may be available by contacting schanzer@BootstrapWorld.org.